Morphology of the Near-Terminator Martian Ionosphere: A Comparison of Models and Data

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Morphology of the near-terminator Martian ionosphere: A comparison of models and data

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We have constructed low and high solar activity models of the Martian thermosphere/ ionosphere for solar zenith angles from 60 to 90° in 5 degree increments. The solar fluxes that we have adopted are those from the Solar 2000 v2.22 models of Tobiska (2004), without enhancements of the soft X-ray fluxes. The background neutral density and temperature profiles are similar to those that we have recently presented (Fox, 2004). We compute the density profiles for 14 ions and nine neutral species. For all the models, we present altitude profiles of the photoionization rates, electron impact ionization rates, total ion production rates, and the predicted electron density profiles. Each model exhibits both an $F_1$ peak and an $E$ peak, although the latter usually appears as a shoulder, rather than as a separate peak. The altitudes of the model peaks are found to be slightly too high. We fit the model peak densities to the equation $n_{i \text{max}, \lambda} = A (\cos \lambda)^k$, where, for an ideal Chapman layer, $A$ is the value of the subsolar peak density, $n_{i \text{max},0}$, and the exponent $k$ is 0.5. We compare the behavior of the model electron density profiles to that of a theoretical Chapman layer and to the values of $A$ and $k$ obtained by fitting the Mars Global Surveyor (MGS) radio science electron density profiles for occultation seasons 1, 2, and 4. We also compare our results to those of previous investigators who have analyzed data from earlier Mars missions and those from MGS and from the Mars Express spacecraft. We find that our model best fit values of $k$ for the $F_1$ peak and those derived from the MGS data are less than the Chapman value of 0.5. We note, however, that the use of spherical geometry alone reduces the value of $k$ below the Chapman value for large solar zenith angles, but the deviation from the experimental values also indicates that there are changes in the neutral atmosphere as the terminator is approached. Our peak densities and predicted subsolar peak densities for both the $F_1$ and $E$ peaks are somewhat smaller than those derived from the data. This is attributed to the use of the S2K v2.22 solar flux models, rather than the S2K v1.24 models or those from Hinteregger (1981). We also evaluate the neutral, ion, and plasma pressure scale heights at the peaks, 33 km above the peaks and at 250 km for all the models. We find that the solar activity variation of our peak densities are in substantial agreement with those determined by other investigators. We argue that the peaks near 90° solar zenith angle are above the photochemical equilibrium region and fitting these peaks to a Chapman profile is therefore inappropriate.


1. Introduction

Electron density profiles of the Martian ionosphere have been recorded by radio occultation experiments aboard several space probes, including Mariners 4, 6, and 7 [e.g., Fjeldbo and Eshleman, 1968; Fjeldbo et al., 1970; Hogan et al., 1972], Mariner 9 [e.g., Kliore et al., 1972a, 1972b, 1973], Mars 2, 3, 4, and 6 [Kolosov et al., 1972, 1973; Vasilev et al., 1975], Vikings 1 and 2 [e.g., Lindal et al., 1979; Zhang et al., 1990], and more recently by the Mars Global Surveyor (MGS) [e.g., Tyler et al., 2001], and Mars Express (MEX) [e.g., Pätzold et al., 2005]. The Mariner 6 and 7 flybys entered the atmosphere during a period of moderately high solar activity ($F_{10,7} \sim 167$ and 187.7, respectively) and at solar zenith angles of $\sim56–57^\circ$. The Mariner 9 orbiter in the primary and extended missions probed the moderate solar activity ionosphere for solar zenith angles from $\sim47$ to 100°, and the Viking orbiters sampled the low solar activity ionosphere in the solar zenith angle (SZA) range from about 53 to 93°. In addition, the Viking 1 and 2 landers, which entered the Martian atmosphere at very low solar activity ($F_{10,7} \sim 70$), carried

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observed in the range $\sim 105$–$135$ km. Figure 1 shows two representative MGS electron density profiles, which were measured on 6 and 7 November 2000, at nearly the same latitudes ($\sim 63^\circ$) and solar zenith angles ($\sim 86^\circ$). The profiles differ significantly on both the topside and the bottomside. In particular, the profile for 6 November 2000 shows a larger more distinct lower peak with a magnitude of about $3 \times 10^3$ cm$^{-3}$, while that for 7 November 2000 shows only a lower shoulder with an estimated peak density of about $1.7 \times 10^5$ cm$^{-3}$.

We will here refer to the upper peak as an $F_1$ peak and to the lower peak as an $E$ peak. This convention is the same as that adopted by Bauer [1973] and by Banks and Kockarts [1977] for the terrestrial ionosphere. The sources of the $F_1$ peak are photoionization by EUV photons with wavelengths of $\sim 150$–$1000$ Å and the concomitant photoelectron impact ionization. The $E$ peak arises from the absorption of solar soft X-ray photons followed by ionization by the high-energy photoelectrons and secondary electrons that are produced. In the terrestrial ionosphere, ionization of O$_2$ by solar Lyman $\beta$ at 1026 Å contributes to the $E$ peak, but this source is not important in the ionosphere of Mars, where O$_2$ is a minor constituent. For the lower peak, electron-impact ionization dominates, while for the upper peak, photoionization is more important [cf., Fox, 2004].

The altitudes at which the peaks have been found to occur have been highly variable. This variability arises from several sources, other than that expected for changes in the solar zenith angle. The peak altitudes have been shown to vary with planetocentric longitude; this variation has been ascribed to planetary scale waves that originate in the lower atmosphere [e.g., Forbes and Hagan, 2000; Bougher et al., 2001; Wilson, 2002; Wilson et al., 2002; Forbes et al., 2002]. This wave activity causes oscillations in the pressure, temperature, and densities of the atmosphere up to altitudes of about 150–160 km [e.g., Keating et al., 1998]. For data from the first MGS occultation season, Bougher et al. [2001] fitted the mass densities at 130 km, and the altitudes of the of the electron density peaks as a function of longitude with spherical harmonics up to wave-3. Bougher et al. [2004] analyzed the first five MGS occultation seasons and found strong wave number 2–3 oscillations in the peak heights as a function of longitude. These oscillations were found to be repeatable over 2 Martian years.

Some of the waves have their origin in topography [e.g., Lindal et al., 1979; Withers et al., 2003; Kliore et al. [1972b]], and more recently, Wang and Nielsen [2004] analyzed the Mariner 9 radio occultation data and showed that the altitude of the peaks rises and falls with the elevation of the surface. This effect has been suggested to be more pronounced at lower latitudes where the variations in the altitude of the surface are larger. Seasonal changes have been predicted to affect the peak altitude, with a variation of about 15 km from aphelion to perihelion [Bougher et al., 2000].

The occurrence of planetwide dust storms has also been known to cause the altitude of the peaks in the electron density profiles to rise by as much as 30 km. This is a result of heating due to absorption of solar energy by the dust particles in the lower atmosphere, which causes the atmosphere to expand, and the altitude of the base of the
thermosphere to rise [e.g., Kliore et al., 1972b; Kliore et al., 1973; McElroy et al., 1977; Stewart, 1987; Keating et al., 1998; Wang and Nielsen, 2003].

[9] Wang and Nielsen [2004] have adduced evidence that the altitude of the electron density peak is modulated also by the interaction of the thermosphere/ionosphere with the solar wind. This mechanism for this interaction is suggested to be the precipitation of solar wind protons, which are predicted to deposit their energy at an altitude of \( \sim 120 \) km [e.g., Kallio and Janhunen, 2001]. Wang and Nielsen showed that the altitude of the \( F_1 \) peak increases with the solar wind proton flux for low values of the proton flux but seems to saturate for proton fluxes greater than \( \sim 3 \) \( \text{cm}^{-2} \text{s}^{-1}\text{ster}^{-1} \). The effect is believed to be more pronounced at larger than at smaller solar zenith angles.

[10] Although the altitudes of the electron density peaks are determined by a number of factors other than photochemistry, the maximum number densities of the \( E \) and \( F_1 \) peaks appear to be under solar control [e.g., Bauer and Hantsch, 1989; Zhang et al., 1990; Hantsch and Bauer, 1990; Fox et al., 1995; Martinis et al., 2003; Mendillo et al., 2003; Rishbeth and Mendillo, 2004]. The measured electron-density profiles have been compared to theoretical Chapman layers by several investigators. Chapman layer theory [Chapman, 1931a] specifically for ionospheres has been described in several textbooks [e.g., Rishbeth and Garriott, 1969; Bauer, 1973; Banks and Kockarts, 1977; Schunk and Nagy, 2000]. We therefore limit ourselves here to a brief presentation of the salient features and the most important equations to define the notation that we use here. These equations are used also to illustrate how the peak number densities change with variations in the parameters in Chapman theory.

[11] A Chapman ion layer is one that is produced by photoionization of a single molecular species, \( XY \), with a rate \( q' (z) \); the resulting molecular ion is destroyed locally by dissociative recombination: \( XY^+ + e \rightarrow X + Y \), with a rate coefficient \( \alpha_{dr} \). The ideal Chapman layer is produced by monochromatic radiation in an isothermal atmosphere, characterized by a temperature \( T_n \). The production rate of the ions is given by

\[
q' (z) = F(z) \sigma' n(z),
\]

where \( n(z) \) is the local number density, \( \sigma' \) is the photoionization cross section, \( F(z) = F_{\infty} \exp[-\tau(z)] \) is the local ionizing solar photon flux, \( F_{\infty} \) is the ionizing photon flux at the top of the atmosphere, and \( \tau(z) \) is the optical depth. If the altitude dependence of the acceleration of gravity \( g \) is ignored, the pressure scale height, which is given by the expression \( H = kTm \), where \( m \) is the mass of the single constituent, is a constant and is equal to the neutral density scale height, \( H_n \). Thus the number density of the neutral species at altitude \( z \) is given by \( n(z) = n_0 \exp(-z/H) \), where \( n_0 \) is the number density at a reference altitude, which may be defined as \( z = 0 \).

[12] The maximum ionization rate in an isothermal atmosphere occurs where the optical depth \( (\tau = nHz E \sec \chi) \) is unity. Here \( E \) is the total absorption cross section, \( \chi \) is the solar zenith angle, and \( nH E \sec \chi = N \sec \chi \) is the slant column density. (Note that we here use \( n \) as the local number density and reserve \( N \) for the column density.) For these conditions, the number density at unit optical depth, \( n = 1/(\sigma' H \sec \chi) \), so the maximum ionization rate in a Chapman layer is

\[
d'_{\text{max}, \chi} = \frac{F_{\infty}}{e} \frac{\sigma'}{\sigma' H \sec \chi} = \frac{q'_{\text{max}, 0}}{\sec \chi}.
\]

Occasionally, for the near-terminator ionosphere, where the plane parallel approximation breaks down, \( \sec \chi \) is replaced by the Chapman Function, \( C_{\chi}(x, \chi) \), where \( x = R/H_n \), \( R \) is the distance from the center of the planet, and \( H_n \) is the scale height at the peak. The Chapman function has been approximated by various combinations of analytical functions [e.g., Chapman, 1931b; Rishbeth and Garriott, 1969; Bauer, 1973]. Chapman functions are not often used in models because of the ease of computing the column densities for spherical geometry numerically, as described, for example, by Rees [1989].

[13] If the altitude of maximum ionization for overhead Sun is defined as \( z = 0 \), then \( n_0 = (\sigma' H)^{-1} \), and, expressing \( F_{\infty} \) in terms of \( q'_{\text{max}, 0} \), the ionization rate as a function of altitude and solar zenith angle is

\[
q'(z) = q'_{\text{max}, 0} \exp \left[ 1 - \frac{z}{H} - \sec \chi e^{-z/H} \right].
\]

At high altitudes (\( z \to \infty \)) the ionization rate profile follows that of the neutral density, and below the peak (\( z \to -\infty \)), the ionization rate rapidly approaches zero. As the solar zenith angle increases, the peak rises and the magnitude of the maximum ion density decreases.

[14] In a Chapman layer photochemical equilibrium (PCE) prevails, so the production rate of the ion is equal to the loss rate due to dissociative recombination:

\[
q'(z) = \alpha_{dr} n'(z) n'(z) = \alpha_{dr} [n'(z)]^2,
\]

where the ion density, \( n'(z) \), is equal to the electron density, \( n'(z) \). The ion or electron density in a Chapman layer is thus given by

\[
n(z) = \left[ \frac{q'(z)}{\alpha_{dr}} \right]^{1/2} = \left[ \frac{q'_{\text{max}, 0}}{\alpha_{dr}} \right]^{1/2} \exp \left[ 1 - \frac{z}{2H} - \frac{1}{2} \sec \chi e^{-z/H} \right].
\]

As equation (5) shows, the maximum ion (or electron) density for overhead sun (\( \chi = 0, z = 0 \)) is given by

\[
n'_{\text{max}, 0} = \left[ \frac{q'(z)_{\text{max}, 0}}{\alpha_{dr}} \right]^{0.5},
\]

and the maximum ion density for a given solar zenith angle \( \chi \) is

\[
n'_{\text{max}, \chi} = n'_{\text{max}, 0} (\cos \chi)^{0.5}.
\]

Equation (5) also indicates that the topside ion scale height should be equal to twice the topside neutral scale height.
The actual Martian electron density profiles are expected to differ from the idealized Chapman profile for several reasons. Electrons are produced by photoionization of a number of different species over a range of photon wavelengths from the EUV to soft and hard X-ray regions, which reach unit optical depth at different altitudes. The altitudes of optical depth unity for solar zenith angles of 60° and 90° over the range 0–2000 Å for both the low and high solar activity models in the Martian thermosphere are shown in Figure 2. The altitudes of unit optical depth in the ~150–1000 Å range show where the photoabsorption rates should peak.

In addition, the lower thermosphere is not isothermal. The values of $T_e$ increase with altitude from the mesopause to the middle thermosphere. The neutral temperatures reach the constant exospheric temperature, $T_{\infty}$, only at high altitudes, which range from ~170 to 200 km in our models. $T_n$ and $T_e$ are equal to the neutral temperature at low altitudes; near the ion peak $T_e$ begins to depart from the neutral temperature; $T_i$ begins to depart from the neutral temperature near 175 km [Hanson et al., 1977]. The value of $T_e$ increases sharply with altitude near and above the ion peak, and reaches a value of ~1200 K near 200 km, and ~2000 K near 230 km [Rohrbough et al., 1979; Chen et al., 1978; Hanson and Mantas, 1988]. The altitude profiles of $T_n$, $T_i$, and $T_e$ assumed in our model are presented in Figure 3.

The plane parallel approximation begins to break down for solar zenith angles greater than about 60°, which includes all of the MGS profiles from seasons 1, 2, and 4. Also, photoionization is supplemented by photoelectron-impact ionization. Because the more energetic photons penetrate to lower altitudes, the electron-impact ionization rate usually peaks lower in the ionosphere than does that due to photoionization. In electron-impact ionization, the electrons are slowed down, but not extinguished, as are photons in photoionization. The major ion produced in the Martian ionosphere, CO$_2^+$, is mostly transformed by reaction with O to produce O$_2^+$ before it can recombine dissociatively. The rate coefficient for dissociative recombination is not a constant, but generally depends on the specific ion and on the value of $T_e$. For O$_2^+$, the major ion in the Martian ionosphere, our adopted value for $\alpha_{O_2^+}$ is $1.95 \times 10^{-7} (300/T_e)^{0.55}$ cm$^3$ s$^{-1}$ for $T_e < 1200$ K, and is proportional to $(300/T_e)^{0.56}$ for $T_e > 1200$ K [Alge et al., 1983; Mehr and Biondi, 1969]. Finally, the temperatures and number density profiles of the background atmosphere are expected to change with SZA.

Given all these caveats, it would be surprising if real electron density profiles were to closely imitate a Chapman layer. All of these effects mentioned will tend to broaden the peak and change its altitude. To determine the degree to which the observed layers exhibit Chapman-like behavior, the measured peak densities as a function of solar zenith angle have often been fitted to the equation

$$n_{\text{max},\chi} = A (\cos \chi)^k,$$

which is analogous to equation (7), but where $k$ and $A$ are treated as free parameters. In Chapman theory for a plane parallel atmosphere, $k = 0.5$ and $A$ is interpreted as the peak electron density at the subsolar point, $n_{\text{max,0}}$, which should be a constant for a given atmospheric model and value of $F \infty$. Equations (2) and (6) show, however, that $n_{\text{max,0}}$ contains some “constants” that are actually variable. In addition to $F \infty$ representing a range of photon wavelengths that reach unit optical depth at different altitudes, $\sigma'$ and $\sigma''$ vary with species and wavelength over the range of ionizing photons; the pressure scale height $H$ should be replaced by $H_n$, which depends on the neutral temperature and its altitude gradient, the acceleration of gravity, and the average mass $m_n$, none of which is constant over the ionospheric layer. At high altitudes, the PCE approximation fails.

Different combinations of radio occultation data sets have been analyzed by several investigators and compared to idealized Chapman layers. Zhang et al. [1990] carried out the most complete analysis of the radio occultation profiles that were available before the MGS mission. Analyses of the variation of electron density profiles with SZA were also made by Hantsch and Bauer [1990].

Other analyses of Martian electron density profiles include that of Bauer and Hantsch [1989], who determined

Figure 2. Optical depth unity as a function of wavelength for the interval 0 to 2000 Å for the 60 and 90° SZA models. (top) High solar activity. (bottom) Low solar activity.

Figure 3. Neutral, ion, and electron temperature profiles assumed in the models. The solid curves are for low solar activity and the dashed curves are for high solar activity.
the solar activity variation of the neutral and plasma scale heights for the available radio occultation profiles. Mendillo et al. [2003] compared the morphology of the two ionospheric layers on Mars with the contemporaneous terrestrial layers; they showed that the peak densities for the two planets were highly correlated. Martinis et al. [2003] modeled MGS data from March 1999 and showed that the day-to-day variability of the observed $F_1$ electron density profiles on Mars closely followed variations in the solar EUV fluxes, as indicated by the $F_{10.7}$ solar EUV proxy. The $E$ peak density was found to exhibit larger variability than could be accounted for by the $F_{10.7}$ index. This is to be expected since the variations of the solar soft X-ray photon fluxes are well known to be larger than those of the EUV fluxes. Rishbeth and Mendillo [2004] carried out same-day comparisons of the peaks of the Martian ionospheric layers, which they named M1 and M2, with the terrestrial $E$ and $F_1$ layers measured by six ionosondes for the same period.

They found that the morphologies and variabilities of the peaks on the two planets were well correlated. Breus et al. [2004] analyzed 732 electron density profiles in the northern hemisphere, and 219 profiles in the southern hemisphere obtained by the MGS Radio Science experiment. They identified the peak electron density and derived the neutral scale height and the value of $T_e$ in the vicinity of the ionization peak for each of the profiles.

We model here the electron density profiles in the Martian ionosphere for solar zenith angles $\chi$ ranging from 60$^\circ$ to 90$^\circ$ for both low and high solar activities. We report the altitudes of the peaks in the production rate profiles and in the total ion or electron density profiles. We then fit the model peak densities to equation (8), and derive values of $A$ and $k$ for each SZA interval, and the overall best fit for the SZA range from 60 to 85$^\circ$. We also compare our values to those we and others have derived from the radio occultation data from MGS and other spacecraft. The neutral and ion density and plasma pressure scale heights in our models, $H_n$, $H_i$, and $H_P$, both near the peak and on the topside, are compared to those derived from the measured electron density profiles and to those appropriate to a Chapman profile. We then compare the low and high solar activity models at comparable solar zenith angles and estimate the variation of the peak densities and the scale heights as a function of $F_{10.7}$.

2. Models

Unlike our previous Mars models, we employ here the Solar 2000 v2.22 solar flux models of W. K. Tobiska (private communication, 2003, 2004) without any enhancement in soft X-ray fluxes. For low solar activity, we adopt the v2.22 76200 fluxes, which are characterized by an $F_{10.7}$ of $\sim$68; for the high solar activity solar fluxes, we adopt the v2.22 99178 fluxes, which are characterized by an $F_{10.7}$ of $\sim$207. The solar photon fluxes that we use are given at 1 Å intervals in the continuum and as delta functions representing the integrated intensities at the strong solar lines, for a total of 1811 wavelengths from 18 to 2000 Å. The S2K v2.2x fluxes are normalized to measurements of the Thermosphere Ionosphere Mesosphere Energetics and Dynamics mission Solar EUV Experiment [e.g., Woods et al., 2000, 2005] and differ significantly from the fluxes from Hinteregger et al. [1981; see also Torr et al., 1979] and the S2K v1.24 fluxes that we have used recently [Fox, 2004; Fox and Faxton, 2005].

For wavelengths less than 18 Å we have adopted the solar fluxes from Ayres [1997, also private communication, 1996]. These harder X ray solar fluxes are highly variable but are absorbed at altitudes below about 100 km, which is outside the region of interest of this model. The effects of variations of hard X rays will treated in another publication.

We have constructed models for solar zenith angles of 60, 65, 70, 75, 80, 85, and 90$^\circ$. We include photoionization, electron-impact ionization, electron-impact excitation, and, for molecules, photodissociation, photodissociative ionization, electron-impact dissociation, and electron-impact dissociative ionization. The range of primary and steady state photoelectron fluxes included is 0–600 eV distributed in 1 eV bins.

Our model is a one-dimensional steady state model in which we include molecular and eddy diffusion for the neutrals and ambipolar diffusion for the ions. The rotation of Mars is included only in computing the value of the effective acceleration of gravity. We compute here altitude density profiles for 14 ions, CO$_2$, Ar, $N_2$, O ($^1S$), O ($^2D$), O ($^2P$), CO, $N^+$, NO$^+$, O$_2$, $O^+$, He, $H^+$, and nine neutral species, including NO, N($^1S$), N($^2D$), N($^2P$), C, H, H$_2$, O($^1D$), and O($^1S$). Our background neutral density profiles for the low and high solar activity models are nearly the same as those we have presented previously [Fox, 2004]. The neutral models consist of altitude profiles of 12 species, including CO$_2$, Ar, $N_2$, O, $O_2$, NO, CO, C, N, H, H$_2$, and He, with densities over the altitude range 80–400 km given in 1 km intervals. In order to compute the local photon fluxes, however, we have extended the background model to 700 km. The major background species for our low solar activity models are based on the Viking I measured densities [e.g., Nier and McElroy, 1976, 1977], and the high solar activity model is based on the Mars Thermospheric General Circulation Model (MTGCM) of Bouger et al. [2000, private communication, 2001] that is appropriate to 60$^\circ$ SZA. In the high solar activity model, we have multiplied the O number densities by 2 so that the mixing ratios are larger than those in the low solar activity model. The resulting O mixing ratios at 130 km are 2% in the low solar activity model, and 3.2% in the high solar activity model. The O mixing ratios in the Venus thermosphere have been shown in various models to vary greatly with solar activity [e.g., Fox and Bouger, 1991]. Bouger et al. [2000] have argued, however, that the O mixing ratio variations over a solar cycle in the Martian thermosphere are limited by dynamical processes, which include large-scale winds and eddy diffusion. There are no in situ measurements of the Martian thermospheric O mixing ratio either at low or high solar activity. O mixing ratios for Viking conditions have been derived from the CO$_2$/O$_2$ ratio of 1–2% at 130 km [e.g., Hanson et al., 1977; Fox and Dalgarno, 1979]. Stewart et al. [1992] have derived smaller global O mixing ratios of $\sim$0.7% from remote sensing of 1304 Å emission intensities from the UV spectrometer on the Mariner 9 orbiter.

We assume here that the background atmosphere is constant with solar zenith angle, except for those minor constituents that we calculate self-consistently in the model,
including N, NO, C, H, and H2. For H and H2, we do not carry out full photochemical calculations. H is assumed to be produced in photodissociation and photodissociative ionization of H2 and also has chemical sources and sinks in our model [e.g., Fox and Sung, 2001; Fox, 2003, 2004]. Because the chemistry of H is not complete, however, we fix the densities at the lower boundaries at 80 km so that H densities at 250 km in the high solar activity model are in the range (2–4) x 107 cm−3, in agreement with the Lyman alpha airglow measured by Mariners 6, 7 and 9 [e.g., Anderson and Hord, 1971; Anderson, 1974]. At low solar activity, the H density in the same altitude range is an order of magnitude or more larger, owing to the smaller escape rate [e.g., Levine et al., 1978; Krasnopolsky, 2002]. H2 is assumed to be characterized by a mixing ratio of 10 ppm at the lower boundary of the model. This value is within the range (15 ± 5) ppm derived by Krasnopolsky and Feldman [2001; see also Krasnopolsky, 2002] from FUSE observations of the Lyman bands of H2. The upper boundary conditions for H and H2 are the Jeans velocities reduced by a factor of about 0.5 to account for the depletion of the high energy tail of the energy distribution [e.g., Shizgal and Blackmore, 1986; Pierrard, 2003].

N and NO are sources of odd nitrogen to the lower atmosphere, and therefore we impose downward fluxes for those species at the lower boundary of the model. Since we do not model the middle atmosphere, we make no attempt to determine accurately the magnitudes of the N and NO fluxes, except that we impose the condition that the fluxes must be small enough so that the densities do not become negative at the lower boundary. The downward fluxes assumed for NO are in the ranges (1–2.5) x 107 cm−2 s−1, and (4–7) x 107 cm−2 s−1, for the low and high solar activity models, respectively. The downward flux of N is assumed to be 100 cm−2 s−1, except for the low solar activity model at 90° SZA, where it is reduced to 10 cm−2 s−1. We assume a zero flux lower boundary condition for C, and fixed density lower boundary conditions for N(P), N(1D), O(1D), and O(S). Zero-flux upper boundary conditions are assumed for the computed neutral species other than H and H2.

For the ions, fixed density lower boundary conditions and upward velocity upper boundary conditions of 1 x 105 cm s−1, and 1.2 x 105 cm s−1 are imposed for low and high solar activities, respectively. The low solar activity upward velocity is that which is found to be necessary to reproduce the Viking I O2 profile [e.g., Chen et al., 1978; Fox, 1993, 1997, 2004; Hanson et al., 1977]. The high solar activity value is roughly that which was required to fit the ratio of the electron density at the peak, 1.8 x 105 cm−3, to that at 300 km, about 7 x 105 cm−3, from the Mariner 6 profile [Fjeldbo et al., 1970]. Upward velocity boundary conditions probably represent upward fluxes at low altitudes and horizontal ion flows at high altitudes. Shinagawa and Cravens [1989] have suggested that an upward flux at the top of a one-dimensional model probably represents the divergence of the horizontal flux of ions, which may be related to the interaction between the solar wind and the ionosphere [e.g., Ma et al., 2004; Lundin et al., 2006]. The imposition of upward velocity boundary conditions affects only the topside scale height, but has little to no effect on the F1 and E peak densities.

While the assumption that background density profiles of the main neutral species do not change with solar zenith angle almost certainly introduces some errors, a comparison of our models with the MGS data and other radio occultation data provides a measure of the accuracy of this assumption.

3. Data Analysis

We have analyzed the MGS radio occultation profiles for seasons 1, 2, and 4, which are all in the northern hemisphere and thus relatively free of the effects of crustal magnetic fields, which are more common in the southern hemisphere. We do not include magnetic fields in our model.
For each day, we analyze one profile which exhibits the median $F_1$ peak for the day. The dates for the above seasons are 24–31 December 1998, 9–27 March 1999, and 1 November 2000 to 6 June 2001, respectively. The SZA assigned to each radio occultation profile is that at 130 km, and the atmosphere sampled over the profile is within 6° or so of the nominal SZA (D. Hinson, private communication, 2006). The solar zenith angle range for these seasons is $\sim71–87°$.

We have divided the data into three solar activity bins. The range of $F_{10.7}$ for bins 1, 2, and 3 are 102–140, 140–190, and 190–273, respectively. The value of $F_{10.7}$ at Mars was adjusted to the orbital position of Mars with respect to that of Earth and to account for the actual Sun–Mars distance compared to that of the mean distance. The logs of the $E$ and $F_1$ peak densities as a function of log (cos $\chi$) are shown in Figures 4, 5, and 6, for bins 1, 2, and 3, respectively. The data points were fitted by a linear least squares regression. The values of the slopes $k$ and the intercepts $A$, from equation (8) were derived from these fits. For $F_{10.7}$ bins 1 and 3, exponents $k$ of 0.42 and 0.49, respectively, were derived for the $F_1$ peaks, and the predicted subsolar peak densities were $1.68 \times 10^5$ and $2.0 \times 10^5$ cm$^{-3}$, respectively. We note, however, that the first and third bins contained only a few profiles, which are not well-distributed in longitude, and thus the characteristics derived from these data have limited validity. Thus we do not include the standard deviations of the peak densities for these bins. For bin 2, which contains 141 data points, we have included the standard deviations in deriving the characteristics of the linear fits. The standard deviations for seven representative data points are included in Figure 5.

The error bars appear large for small peak magnitudes, but for the densities that approach $\sim10^5$ cm$^{-3}$, the error bars are barely visible on the plots, which are logarithmic. The derived value of $k$ is $0.465 \pm 0.010$ and the value of $A$ is $(1.82 \pm 0.03) \times 10^5$ cm$^{-3}$ for the $F_1$ peaks. The median values of the $F_1$ peak densities for $F_{10.7}$ bins 1, 2, and 3, are $9.74 \times 10^4$, $8.70 \times 10^4$, and $1.08 \times 10^4$ cm$^{-3}$, respectively.

We also analyzed the lower $E$ peaks. Locating the altitude and magnitude of the lower peak was found to be difficult when it was observed as only as a shoulder, so these quantities were determined by visual inspection of the profiles. Although this procedure obviously limits the accuracy of both the peak densities and altitudes somewhat, we concluded that it was better than attempting to identify an inflection point in inherently noisy data. For the lower peak or shoulder, slopes $k$ of 0.55 and 0.53 and intercepts $A$ of $8.9 \times 10^4$ and $9.6 \times 10^4$ cm$^{-3}$, were determined for bins 1 and 3, respectively. For bin 2, we have included the standard deviations of the peak magnitudes and derive a slope of $0.551 \pm 0.024$ and an intercept of $(9.4 \pm 0.4) \times 10^4$ cm$^{-3}$. The median values for the $E$-peak densities are $4.1 \times 10^4$, $3.9 \times 10^4$, and $4.5 \times 10^4$ cm$^{-3}$, for bins 1, 2, and 3, respectively. With the addition of the fifth, sixth, and seventh occultation seasons, more profiles should be added, and the parameters will be more accurately determined.

### 4. Model Results

#### 4.1. Peak Altitudes

Altitude profiles of the predicted photoionization rates, electron-impact ionization rates, total production rates of ions, and peak densities for a range of solar zenith angles for low and high solar activities are shown in Figures 6 to 9. The altitude range of 80 to 220 km was chosen for presentation because it is approximately that for which the MGS RS electron densities have been reported. There are seven curves on each figure, which are, in order of decreasing peak density and increasing peak height, those appropriate to solar zenith angles of 60, 65, 70, 75, 80, 85, and 90°. The altitudes of peak production and peak electron densities for all the models for the $F_1$ and $E$ regions are summarized in Tables 1 and 2, respectively.

The computed photoionization rates as a function of altitude and solar zenith angle are shown in Figure 7. For the low solar activity models, the profiles exhibit an upper peak that rises from 134 to 149 km, and a lower peak that rises from 109.5 to 123.5 km as the SZA increases from 60 to 85°. For the high solar activity models, the photoionization rate profiles exhibit an upper peak that rises from 136 to 186 km. The altitudes of peak production and peak electron densities for all the models for the $F_1$ and $E$ regions are summarized in Tables 1 and 2, respectively.

#### Table 1. Predicted Altitudes of the $F_1$ Peak Ion Densities and Production Rates as a Function of Solar Zenith Angle (SZA), km

<table>
<thead>
<tr>
<th>SZA</th>
<th>Ion Density</th>
<th>Photo Production</th>
<th>Electron Impact Production</th>
<th>Total Production</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Low Solar Activity</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
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<td>90°</td>
<td>178</td>
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<td>158</td>
<td>165</td>
</tr>
</tbody>
</table>
158 km, and a lower peak that rises from 114 to 126.5 km as the SZA increases over the same range. A large increase is observed in the altitudes of peak photoionization between the solar zenith angles of 85 and 90° for both models. At high altitudes the photoproduction rate profiles merge together, as would be expected as the optical depth approaches zero. In the models, we identify the altitude of a lower shoulder in the production rate and density profiles as that for which the differences between the values at adjacent altitudes is a minimum. Thus because our altitude increment is 1 km, the altitude of the shoulder may be expressed as located at the nearest half kilometer, but high accuracy is not assigned to these values.

[35] Computed altitude profiles of the production rates from electron-impact ionization are shown in Figure 8 and those for the total ionization rates are shown in Figure 9. The electron impact production rate profiles exhibit two peaks that are comparable in magnitude. The upper peaks in the photoelectron impact ionization profile are below those of the photoproduction rate peaks by 6–13 km. Photoionization dominates the ion production for the $F_1$ peak, and the upper peaks in the total production rate profiles are found to be slightly below those for photoionization. For the $E$ peak, impact of photoelectrons and secondary electrons dominates and the altitude of total production is near that for electron impact. The computed electron density profiles for low and high solar activity models as a function of SZA are shown in Figure 10.

[36] The model $F_1$ peak rises from 136 to 149 km at low solar activity, and from 137 to 158 km at high solar activity, as the solar zenith angle increases from 60 to 85°. The largest increases in the $F_1$ peak altitudes are from 85 to 90° SZA, where the peak is predicted to rise by 8–20 km. The $F_1$ peak densities are found to occur slightly above the altitudes of peak production process for the following reasons. As mentioned previously, the dissociative recombination rate coefficient of the major ion $O_2$ has a negative electron temperature dependence. In the $F$-region, $T_e$ increases significantly with altitude (cf., Figure 3), and therefore the $O_2$ loss rates decrease with altitude. Thus the electron densities are larger and the peaks are higher than those that would be expected for an altitude-independent $T_e$ profile. This is especially true for the high solar activity 90° SZA peak, which appears 13 km above the total production peak. Figure 9 shows that there is a shoulder near 168.5 km, which is associated with the peak production rates. Owing to the rapid rise of $T_e$ in this region, however, the absolute maximum appears near 178 km. We note also that the $O_3$ PCE boundary for the high solar activity 90° SZA model is near 160 km, so the predicted $F_1$ peak is above the PCE region. For the other models, the $O_3$ PCE boundary varies from ~170 km for the 90° SZA low solar activity model to ~180 km for both high and low solar activity 60° SZA models.

[37] The predicted altitude of the $E$ electron density peak or shoulder rises over the SZA range of 60 to 85° from 110 to 123 km in the low solar activity model and from 115 to 128 km in the high solar activity model. The predicted increase in the $E$ peak altitude from 85 to 90° SZA is in the range 7–9 km.

[38] It is difficult to compare the altitudes of the model peaks with the radio occultation data. The data from Mariners 4, 6, and 7, Vikings 1 and 2, and the Mariner 9 extended mission showed $F_1$ peak densities at lower altitudes, in the range ~120–150 km for the SZA range from 60 to 85° [e.g., Zhang et al., 1990]. Our analysis of the MGS data from seasons 1, 2, and 4 showed that the $F_1$ peak altitudes vary from 125 to 148 km over the SZA range 71–87°. By contrast, the $F_1$ peaks for the 70 to 85° SZA models increase from 139 to 149 km at low solar activity and from 142 to 158 km at high solar activity.

[39] At 90° SZA, our model $F_1$ electron density peaks are at 157 and 178 km, for low and high solar activity.

Table 2. Predicted Altitudes of the $E$-Region Peak Densities and Ion Production Rates as a Function of Solar Zenith Angle, km

<table>
<thead>
<tr>
<th>SZA (°)</th>
<th>Ion Density</th>
<th>Photo Production</th>
<th>Electron Impact Production</th>
<th>Total Production</th>
</tr>
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<tbody>
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High Solar Activity

<table>
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<th>Electron Impact Production</th>
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Figure 7. Altitude profiles of the photoionization rates for all the models. The curves are, in order of decreasing peak photoionization rate and increasing peak altitude, those for the 60, 65, 70, 75, 80, 85, and 90° models. (top) Low solar activity. (bottom) High solar activity.
respectively. There are very few electron density profiles for solar zenith angles near 90° to compare to our models. A few RO profiles from the Viking 2 orbiter were in the range 89–94° [Zhang et al., 1990]. These orbits were at low solar activity. They show that the range of peak altitudes are similar to our predictions, about 150–180 km. A large increase in the peak altitudes to values in the 180 to 200 km range seems to occur for solar zenith angles greater than 93°. Four Mariner 9 ingress profiles exhibited solar zenith angles in the range 89–100°. The peak densities, however, also appear to be in the 150–180 km range. The error incurred by assuming spherical symmetry in retrieving radio occultation electron density profiles should maximize near 90° SZA, but the impact on the profiles is difficult to ascertain. A selected profile from the MARSIS instrument on MEX for an SZA of 89.3°, however, showed a peak at 195 km [Gurnett et al., 2005], which is significantly higher than our 90° SZA model peaks.

Since the heights of the measured peaks are determined by many factors other than photochemistry, the higher peaks in the MGS data do not necessarily correspond to larger solar zenith angles. Our models do not include the strong longitudinal variation of peak height, which results from wave activity or dust loading in the lower atmosphere.

Bougher et al. [2001] found that for the first MGS occultation season, where the solar zenith angle range was 79 to 81°, the average $F_1$ peak height was 134.4 km, and the lower peak was found in the altitude range 110–115 km. Solar activity for this occultation season was moderate, with an $F_{10.7}$ value ranging from ~130 to 170. Bougher et al. [2004] analyzed the first five data sets, and reported a mean $F_1$ peak height in the range ~133.5–135 km for solar zenith angles from 78–82°. By contrast, the 80° SZA model $F_1$ peak altitudes appear in the range 144–148 km, and the $E$ peak altitudes appear in the range 117–122 km, where the lower value is for low solar activity and the higher value is for high solar activity.

The Mariner 9 radio occultation measurements at orbital insertion occurred during a planetwide dust storm, and the altitudes of the peaks were found to be in the range 135 to 155 km for solar zenith angles of ~50 to 60°. Our 60° solar zenith angle models exhibit $F_1$ peaks near 136–137 km for nondusty conditions. Thus it appears that compared to the existing radio science data for solar zenith angles that are less than 85° and nondusty conditions, our model peak altitudes are too high by ~5–10 km.

It is possible that our exospheric temperatures are too large near the terminator, and there may be a small vertical offset for all the models. O is the major constituent of the models at altitudes above 195 and 209 km in the low and high solar activity models, respectively. Since we have doubled the O densities in the high solar activity model, this might be expected to result in somewhat higher electron density peaks. A comparison to our previous model shows that the effect is negligible [Fox, 2004]. It is also possible that the absorption cross sections that we adopted are too large. A review of the absorption cross sections for CO$_2$ and O has not, however, revealed any significant uncertainties. Small differences from other recent models may arise because our models contain 12 absorbing species, rather

**Figure 8.** Altitude profiles of the electron impact ionization rates for all the models. The ionization rates include those produced by photoelectrons, and those produced by secondary and subsequent electrons. The curves are, in order of decreasing peak production rate and increasing peak altitude, those for the 60, 65, 70, 75, 80, 85, and 90° models. (top) Low solar activity. (bottom) High solar activity.

**Figure 9.** Altitude profiles of the total ionization rates for all the models. The curves are, in order of decreasing peak production rate and increasing peak altitude, those for the 60, 65, 70, 75, 80, 85, and 90° models. (top) Low solar activity. (bottom) High solar activity.
than only 2 to 6 species, and our upper altitude for computing the photoabsorption rate is 700 km. Because the altitudes of the peaks do appear to increase as the solar zenith angle increases, as measured by the pre-MGS radio occultation experiments [e.g., Zhang et al., 1990; Hantsch and Bauer, 1990], the MGS data [cf. Breus et al., 2004], and the recent MARSIS data [Gurnett et al., 2005], it appears that the slant column densities for unit optical depth do occur at higher altitudes as the SZA increases, but not as high as our SZA invariant model.

By contrast, we note that radio occultation profiles measured by the Pioneer Venus (PV) Orbiter Radio Occultation (ORO) experiment show that the altitude of the main electron density peak in the Venus ionosphere remains approximately constant at about 140 km as the solar zenith angle increases from 80° to 85° [Cravens et al., 1981]. This non-Chapman behavior has been ascribed to the collapse of the thermosphere as the daytime thermosphere merges into the nighttime cryosphere. (The magnitudes of the Venusian electron density peaks as a function of solar zenith angle were found, however, to be approximately Chapman-like.)

Thus the Martian thermosphere does not appear to “collapse” with increasing SZA, as does that of Venus. That the altitudes of the model peaks are higher than those of the MGS RS profiles, however, indicates that the assumption of a constant background atmosphere is not justified. There are probably some decreases in the thermospheric temperatures and the neutral densities as the solar zenith angle increases. In particular, the MTGCM shows that there appear to be large changes in the neutral atmosphere for solar zenith angles near 90° compared to those for smaller solar zenith angles (S. Bougher, private communication, 2006).

Breus et al. [1998] constructed a model in which the diurnal variations of the Martian exospheric temperatures were chosen to approximate the diurnal variations in an early MTGCM of Bougher et al. [1990]. For high solar activity (F10.7 = 200), the exospheric temperatures decreased from ~320 to 260 K as the local time in the model changed from 1600 to 2000 hours. For low solar activity (F10.7 = 70), the exospheric temperature decreased from ~200 to 160 K over the same local time period. By fitting the electron density profiles with Chapman functions, Breus et al. [2004] found that Hn at the ion peak varied from about 6 to 15 km, but the variability was not strongly correlated with SZA. They found that Hn decreased by only 0.12 km/degree over the SZA range 75 to 87°, and suggested that the variation of the atmosphere near the peak was less than that above the peak.

The predicted maximum total ion densities, neutral and electron temperatures, and neutral scale heights at the peaks of the electron density profiles in the F1 and E models are shown in Tables 3 and 4, respectively. The neutral scale heights were calculated numerically from the model densities and are not equal to the pressure scale heights, which are computed as kT/(mua).

Table 3 shows that the model neutral scale height at the F1 peak increases from 9.0 to 9.8 km in the low solar activity model, as the solar zenith angle increases from 60 to 85° SZA. The values of Hn for the low solar activity F1 peak are in substantial agreement with that determined from Viking electron density profile by Bauer and Hantsch [1989] of 9.5 km for a solar zenith angle of 45°, and of 10 km by Hantsch and Bauer [1990] for a selection of pre-MGS data. The model high solar activity neutral scale heights at the peaks are in the range 8–15.2 km and increase with increasing SZA. A scale height of 11 km was derived from the Mariner 6 data by Bauer and Hantsch [1989]. The Mariner 6 ingress electron density profile corresponds, however, to a smaller solar zenith angle of 56–57°. The scale heights in our 60° SZA models range from 8 to 9 km. We find that the neutral scale height at the F1 peak increases only slowly with SZA for values less than about 80°, in qualitative agreement with Breus et al. [2004].

Table 4 shows that for the low solar activity model at the E peak, the scale height ranges from 7.2 to 8.7 km for the SZA range of 60 to 90°; similarly, for the high solar activity model, the value of Hn at the peak varies between 7.1 and 8.0 km.

We note here that there are inherent uncertainties in determining Hn by fitting the radio occultation electron density peak profiles to a Chapman layer peak (equation (5)), as has been done by Bauer and Hantsch [1989] and by Breus et al. [1998, 2004]. As mentioned previously, and as Figure 2 shows, ionization is produced by photons characterized by a large range of wavelengths that reach unit optical depth at different altitudes. In addition, ionization is also produced by impact of photoelectrons and secondary electrons, which tend to deposit their energy below that of photons, as shown in Tables 1 and 2. The thermosphere is not isothermal. The effect of the Tn dependence of the dissociative recombination rate tends to cause the peak

Figure 10. Altitude profiles of the total electron densities for all the models. The curves are, in order of decreasing peak density and increasing peak altitude, those for the 60, 65, 70, 75, 80, 85, and 90° models. (top) Low solar activity. (bottom) High solar activity.
to rise above that for a temperature independent ion loss rate. Thus the ion density profile near the peak is inherently broader and has a different shape than that of a theoretical Chapman peak.

[51] From a study of the electron density profiles from the Mariners 4, 6, 7, and 9 and the Viking landers, Bauer and Hantsch [1989] proposed that the neutral temperature at the F₁ peak did not vary as much as the exospheric temperature over a solar cycle. They found that at the electron density peak, \( H_n \propto F₁^{1.6} \). A comparison of our model values of \( H_n \) for high and low solar activities at various solar zenith angles leads to exponents of \( F₁^{1.7} \) that vary from −0.11 to 0.45. This difference is largely a result of using different shapes for our low and high solar activity neutral temperature profiles and of having only two data points for each SZA.

### 4.2. Peak Densities

[52] The computed density maxima for the F₁ and E peaks for the low and high solar activity models are plotted as a function of \( \cos \chi \) from 60° to 90° in Figure 11. As the SZA increases from 70 to 85°, the approximate range of the MGS RS data, the magnitudes of the predicted \( F₁ \) peaks decrease from \( 7.2 \times 10^4 \) to \( 4.4 \times 10^4 \) cm⁻³ at low solar activity, and from \( 1.05 \times 10^5 \) to \( 6.1 \times 10^3 \) cm⁻³ at high solar activity. The E peaks decrease from \( 3.5 \times 10^4 \) to \( 1.9 \times 10^4 \) cm⁻³, and from \( 5.5 \times 10^3 \) to \( 3.0 \times 10^3 \) cm⁻³, for the low and high solar activity models, respectively, over the same SZA range.

[53] We can compare our model peak densities at 80° SZA to those determined by Bouger et al. [2001] for the first MGS occultation season, for which solar activity was moderate, and the solar zenith angle was 79–81°. Bouger et al. reported a mean \( F₁ \) peak density of \( 8.1 \times 10^4 \) cm⁻³ and an \( E \) peak density of \( 4 \times 10^5 \) cm⁻³. The mean \( F₁ \) peak densities derived from the first five MGS data sets by Bouger et al. [2004] were in the range (7.3–8.5) \times 10^4 \) cm⁻³ for solar zenith angles of 78–82° and moderate solar activity. Our model values for both peak densities at 80° SZA are somewhat smaller: the \( F₁ \) peak densities are \( (5.6–7.8) \times 10^4 \) cm⁻³, and the \( E \) peak densities are

### Table 3. Characteristics of Model Electron Density \( F₁ \) Peaks for Low and High Solar Activities

<table>
<thead>
<tr>
<th>SZA</th>
<th>Maximum Density, cm⁻³</th>
<th>Predicted ( k )</th>
<th>Predicted ( n_{\text{peak},0} ), cm⁻³</th>
<th>( T_n ), K</th>
<th>( T_e ), K</th>
<th>Scale Height km</th>
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<td>141</td>
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<td>192</td>
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<td>1.08(5)</td>
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<td>200</td>
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<td>227</td>
<td>8.0</td>
</tr>
<tr>
<td>65°</td>
<td>1.17(5)</td>
<td>0.49</td>
<td>1.78(5)</td>
<td>196</td>
<td>246</td>
<td>8.1</td>
</tr>
<tr>
<td>70°</td>
<td>1.05(5)</td>
<td>0.46</td>
<td>1.72(5)</td>
<td>214</td>
<td>282</td>
<td>9.6</td>
</tr>
<tr>
<td>75°</td>
<td>9.3(4)</td>
<td>0.45</td>
<td>1.70(5)</td>
<td>222</td>
<td>302</td>
<td>9.7</td>
</tr>
<tr>
<td>80°</td>
<td>7.8(4)</td>
<td>0.37</td>
<td>1.41(5)</td>
<td>237</td>
<td>337</td>
<td>10.7</td>
</tr>
<tr>
<td>85°</td>
<td>6.1(4)</td>
<td>-</td>
<td>-</td>
<td>261</td>
<td>410</td>
<td>15.2</td>
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<tr>
<td>90°</td>
<td>4.7(4)</td>
<td>-</td>
<td>-</td>
<td>288</td>
<td>531</td>
<td>17.6</td>
</tr>
</tbody>
</table>

aRead as \( 1.11 \times 10^4 \).

### Table 4. Characteristics of Model Electron Density \( E \)-Region Peaks for Low and High Solar Activities

<table>
<thead>
<tr>
<th>SZA</th>
<th>Maximum Density, cm⁻³</th>
<th>Predicted ( k )</th>
<th>Predicted ( n_{\text{peak},0} ), cm⁻³</th>
<th>( T_n ), K</th>
<th>( T_e ), K</th>
<th>Scale Height km</th>
</tr>
</thead>
<tbody>
<tr>
<td>0°</td>
<td>6.2(4) a</td>
<td>0.52</td>
<td>-</td>
<td>139</td>
<td>139</td>
<td>7.3</td>
</tr>
<tr>
<td>60°</td>
<td>4.3(4)</td>
<td>0.53</td>
<td>6.3(4)</td>
<td>140</td>
<td>140</td>
<td>7.2</td>
</tr>
<tr>
<td>65°</td>
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<td>140</td>
<td>7.2</td>
</tr>
<tr>
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<td>3.5(4)</td>
<td>0.51</td>
<td>6.1(4)</td>
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<td>140</td>
<td>7.4</td>
</tr>
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<td>3.1(4)</td>
<td>0.49</td>
<td>6.0(4)</td>
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<td>7.5</td>
</tr>
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</tr>
<tr>
<td>85°</td>
<td>1.9(4)</td>
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<tr>
<td></td>
<td><strong>High Solar Activity</strong></td>
<td></td>
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<td></td>
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<td>133</td>
<td>7.2</td>
</tr>
<tr>
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<td>0.49</td>
<td>9.3(4)</td>
<td>134</td>
<td>134</td>
<td>7.3</td>
</tr>
<tr>
<td>65°</td>
<td>6.1(4)</td>
<td>0.49</td>
<td>9.3(4)</td>
<td>134</td>
<td>134</td>
<td>7.3</td>
</tr>
<tr>
<td>70°</td>
<td>5.5(4)</td>
<td>0.48</td>
<td>9.2(4)</td>
<td>135</td>
<td>135</td>
<td>7.2</td>
</tr>
<tr>
<td>75°</td>
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<td>0.46</td>
<td>9.0(4)</td>
<td>136</td>
<td>136</td>
<td>7.1</td>
</tr>
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<td>0.40</td>
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<td>140</td>
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<td>-</td>
<td>-</td>
<td>155</td>
<td>155</td>
<td>7.4</td>
</tr>
<tr>
<td>90°</td>
<td>2.2(4)</td>
<td>-</td>
<td>-</td>
<td>189</td>
<td>241</td>
<td>8.0</td>
</tr>
</tbody>
</table>

aRead as \( 6.2 \times 10^4 \).
are $(2.5–4.0) \times 10^4 \text{ cm}^{-3}$ where the range is from low to high solar activities. [54] Martinis et al. [2003] analyzed the second MGS RS season, which consists of 17 electron density profiles obtained between 9 and 27 March 1999. The values of $F_{10.7}$ during this time period varied from 105 to 153. The MGS main peak densities were in the range $(7–9) \times 10^4 \text{ cm}^{-3}$. They modeled the densities using the S2K v1.24 solar fluxes of Tobiska [2004] and predicted an $F_1$ peak density of $8.5 \times 10^4 \text{ cm}^{-3}$. The median $F_1$ peak density that we derived for MGS occultation seasons 1, 2, and 4, for higher solar activity conditions ($F_{10.7} = 140–190$) is $8.7 \times 10^4 \text{ cm}^{-3}$.

[55] Thus compared to the measurements and other models, it appears that our predicted peak densities are somewhat too small. The use of the S2K v2.22 solar flux model of Tobiska [2004] in general gives ion peak densities that are 20–30% smaller than those computed with the S2K v1.24 models, or with the Hinteregger solar flux models, which we have used previously [e.g., Fox, 2004]. For example, the model $F_1$ peak density for the present 60° SZA S2K v2.22 high solar activity model is $1.27 \times 10^5$, but increases to $1.76 \times 10^5 \text{ cm}^{-3}$ when the S2K v1.24 solar fluxes are adopted. There is a similar discrepancy between the measured and model electron density profiles for Venus computed with the S2K v1.24 and v2.22 fluxes [e.g., Fox and Paxton, 2005; J. Fox, submitted manuscript, 2006].

[56] We fitted the model peak densities for each 5° solar zenith angle interval to equation (8), and derived values of the exponent $k$ and intercept $A$ ($n_{i,\text{max}}^i$), which are shown at the lower solar zenith angle for each interval in Tables 3 and 4. There are no predictions for the interval 85–90° because cos(90°) is zero, and, as most investigators, we do not use a Chapman function for the inverse cosine. The values computed for the 0° SZA models are shown for reference only. For the $F_1$ peak, as the solar zenith angle increases from 60 to 85°, the values of $k$ decrease from 0.38 to 0.34 at low solar activity, and from 0.51 to 0.37 at high solar activity. The decrease in the value of $k$ as the SZA interval increases reflects, in part, the increasing effect of spherical geometry as the terminator is approached. This is because the plane parallel approximations on which equations (2) and (7) are based, break down near the terminator. The column densities above a given altitude for a given SZA are smaller for a spherical atmosphere than for a plane parallel atmosphere, and thus the values of $n_{i,\text{max}}^i$ derived from models of the near terminator ionosphere are not expected to exhibit high accuracy. The predicted values of $n_{i,\text{max}}^i$ are in the ranges $(1.0–1.1) \times 10^5$ and $(1.4–1.8) \times 10^5 \text{ cm}^{-3}$ for the low and high solar activity models, respectively.

[57] In Figure 12, $\log n_{i,\text{max}}^i$ is plotted against log cos $\chi$ for solar zenith angles 60 to 85°, and the linear least squares fit to each set of model electron density peaks is also shown. The models for solar zenith angles of 0 and 90° are excluded from this fit. The slopes of the lines are the exponents $k$ in equation (8) and the curves are labeled by the values for each set of calculations. For the model $F_1$ peak, the best fit values of $k$ are 0.45 and 0.43, for low and high solar activities, respectively.

[58] For the $E$ peak, the computed values of $k$ decreases from 0.53 to 0.42 for the low solar activity model, and from 0.49 to 0.40 for the high solar activity model, as the SZA intervals increase from 60–65° to 80–85°. The individual intervals for 75° or less yield values for $k$ that appear to be close to the “Chapman” value of 0.5. Since for the near-terminator ionosphere we expect smaller values of $k$ for the Chapman expression (8), a value of 0.5 is actually “non-Chapman.” When all the $E$ peak densities for the solar zenith angle range 60–85° are plotted against SZA, the overall slopes of the linear least squares fits are 0.43 and 0.45 for the low and high solar activity models, respectively. The predicted values for $n_{i,\text{max}}^i$ decrease from $6.3 \times 10^4$ to $5.3 \times 10^4 \text{ cm}^{-3}$ at low solar activity and from $9.3 \times 10^4$ to $8.1 \times 10^4 \text{ cm}^{-3}$ at high solar activity, from the 60–65° to the 80–85° SZA intervals.

[59] Our model best fit values for $k$ at the $F_1$ peak of 0.45 and 0.43 for low and high solar activities, respectively, are slightly smaller than that derived from the moderate solar activity MGS data (0.465 ± 0.010). This may be due in part to the assumed model-invariant electron temperature profile, which results in increases in $T_e$ with SZA at the peaks. At the $F_1$ peak, $T_e$ increases from 192 to 331 K at low solar activity, and from 237 to 531 K at high solar activity as the SZA increases from 60 to 90°. The largest increase is from 85 to 90° SZA. As stated previously, larger values of $T_e$ at the peak increase the peak density and partially compensate.

![Figure 11](image1.png)

**Figure 11.** Model $F_1$ and $E$ peak densities as a function of cos(SZA). The circles are those for high solar activity and the squares are for low solar activity. The filled symbols are the $F_1$ peaks and the open symbols are the $E$ peaks.

![Figure 12](image2.png)

**Figure 12.** Log-log plot of model peak density as a function of cos(SZA). The symbols are as in Figure 11. The best fit linear regressions are shown. The curves are labeled by the slopes, $k$. 
for the decrease in ion densities that arises from the increase of SZA. Equations (2) to (6) show that the maximum densities should be inversely proportional to $H_n^{0.5}$ and proportional to $T_e^{0.35}$. Since the two parameters at the $F_1$ peaks in the model increase as the solar zenith angle increases, the overall effect is that variations in the parameters would be expected to cancel each other out somewhat. [60] Nevertheless, the model $F_1$ peaks do not seem to follow Chapman theory as expressed by equation (7). More important, however, is that the exponents $k$ for the model $F_1$ peaks are significantly smaller than the values (0.5–0.57) derived by previous investigators. The solar zenith angle range of the data analyzed by, for example, Hantsch and Bauer [1990] and Zhang et al. [1990] was larger, and they derived $k$ values of 0.57 from the existing pre-MGS electron density profiles. Martinis et al. [2003], however, analyzed solar zenith angle variations of the $F_1$ peak for the second season of MGS data, which is in the near terminator region, and found that they approximated that of a Chapman layer, with $(\cos \chi)^{0.5}$. Unless the precision of the $k$ value derived by Martinis et al. was limited to one decimal place, their value is slightly larger than our derived value of $0.465 \pm 0.010$ for the MGS peaks for the $F_1$ peak range 140–190, which is in turn slightly larger than the values 0.43 and 0.45 derived from our high and low solar activity models, respectively. [61] Table 4 shows the variation in the neutral and electron temperatures and in the neutral scale heights as a function of SZA for the model $E$ peaks in the 60 to 90° range. The temperature variations are small for solar zenith angles of 85° or less at low solar activity, and for solar zenith angles less than 80° at high solar activity. These characteristics by themselves would tend to result in “Chapman-like” behavior, and a coefficient $k$ closer to ~0.5 at low solar activity, although the characteristics of $E$ layers are such that we expect them to be less Chapman-like than the $F_1$ layers. We find, however, that the overall best fit values for $k$ are 0.43 for low solar activity and 0.36 for high solar activity at the $E$ peaks. Both values are, however, significantly smaller than the value $0.551 \pm 0.024$ derived from the MGS data. This model values of $k$ reflect in part variations in the assumed values of $T_e$ and in $H_n$. As mentioned previously, we also expect that the use of spherical rather than plane parallel geometry in models in the near terminator region would reduce the value of $k$ below the value 0.5 for the ideal Chapman layer as expressed by equation (7), even if the other parameters are assumed to be Chapman-like. For spherical geometry, the computed peak electron densities are larger than those for a plane parallel atmosphere, and thus the SZA dependence of $k$ is decreased. That this effect increases in importance as the solar zenith angle approaches the terminator is shown in Tables 3 and 4, where the derived values of $k$ decrease with increases in the solar zenith angle ranges. The discrepancy between the model values of $k$ and those derived by fitting to the MGS data, however, constitutes significant evidence that there are changes in the thermosphere as a function of SZA that are not reflected in the model. [62] The error produced by the effect of spherical geometry can be reduced by substituting a Chapman function $C(h, \chi)$ for the sec $\chi$ [e.g., Chapman, 1931b]. The assumed parameters in the Chapman function fitted by Gurnett et al. [2005] to the 14 August 2005 MARSIS electron density profile at a solar zenith angle of 89.3° were $H_n = 25$ km and $x = 141$, and the resulting value of $C(h, \chi)$ was 13.5. The value of the Chapman function can be compared to the ratio of the numerically integrated neutral densities above 195 km at 90° to those at 0° of 15.5 in our low solar activity model. Our model value of $H_n$ at 195 km of 15.8 km is, however, significantly smaller than that assumed by Gurnett et al. [2005]. [63] The predicted subsolar $F_1$ peak densities, $A = n_{\text{max},0}$, derived from our linear fits to Equation (8) to the model peaks shown in Figure 12 are $1.07 \times 10^5$ and $1.68 \times 10^5$ cm$^{-3}$, for low and high solar activities, respectively; the analogous predicted subsolar $E$ peak densities are $5.9 \times 10^6$ and $8.9 \times 10^7$, respectively. The values of the $F_1$ subsolar peak densities are consistent with those derived by Bauer and Hantsch [1989] of $1 \times 10^5$ cm$^{-3}$ for Viking (low solar activity) conditions and $1.6 \times 10^5$ cm$^{-3}$ for Mariner 6 (moderately high solar activity) conditions. Zhang et al. [1990], however, derived somewhat larger subsolar $F_1$ peak densities of (1.5–2.3) $\times 10^5$ cm$^{-3}$ from their analysis of pre-MGS data. Similarly, Hantsch and Bauer [1990] derived a single value for $n_{\text{max},0}$ of $2 \times 10^5$ cm$^{-3}$. Breus et al. [1998, 2004] reported larger values for Viking and Mariner 9 conditions (low to moderate solar activity) of $(1.77–1.97) \times 10^5$ cm$^{-3}$. [64] Gurnett et al. [2005] fitted the 89.1° SZA MEX MARSIS profile from 14 August 2005 to a Chapman profile, and predicted a subsolar peak electron density of $1.32 \times 10^5$ cm$^{-3}$ at an altitude of 130 km. As mentioned previously, in our model, the upper boundary of the PCE region for the 90° low solar activity model is near 170 km. Thus fitting this profile to a Chapman layer, even if the sec $\chi$ is replaced by a Chapman function, may be inappropriate. Gurnett et al. also derived a best fit subsolar maximum electron density for all of the profiles for 12 MEX orbits between 5 July 2005 and 10 October 2005, and reported a fairly high value of $1.98 \times 10^5$ cm$^{-3}$. This whole period was one of generally low solar activity, with $F_{10.7}$ ranging from about 73 to 130. [65] A major reason for the discrepancy between the parameters $k$ for the $F_1$ and $E$ peak densities derived from the data and those of our models is that our model values for $T_e$ at the ion peaks may be unrealistically high. Owing to the assumption of a constant $T_e$ profile for all the models, the value of $T_e$ at the $F_1$ peak increases significantly for both the low and high solar activity models as the SZA increases. As the values of $T_e$ increase, the ion loss rates decrease, leading to larger ion peak densities. Thus a smaller variation of the peak densities with solar zenith angle would be predicted, which translates into smaller model values of $k$. [66] The Martian ion temperature profiles were only measured by the Viking RPAs during solar minimum for a solar zenith angle of ~45° [Hanson et al., 1977]. Hanson and Mantas [1988] reported values of $T_e$ measured by the Viking RPA’s above 200 km. Calculations of electron temperature profiles were made by Chen et al. [1978] and Rohrbaugh et al. [1979]. Our assumed values for $T_e$ below 200 km are based on the latter calculations. It has been found to be difficult to model the plasma temperatures without imposing an ad hoc heat source at the top of the
models [e.g., Johnson, 1978; Chen et al., 1978; Choi et al., 1998; Nagy and Cravens, 2002].

In the lower thermosphere/ionosphere, where the neutral number densities are large and collisions are frequent, \( T_n \), \( T_e \), and \( T_a \) are equal. The ambient electrons are heated by collisions with the suprathermal electrons produced in photoionization, and the departure of the electron temperature profile from the neutral temperature profile probably occurs near the ionization peak, which rises with solar zenith angle. Our electron temperatures begin to diverge (unrealistically) from the neutral temperatures near 130 km in all the models. The electrons cool by excitation of the fine structure levels of \( \text{O}(\lambda P_{2,1,0}) \), by downward conduction, and by coulomb collisions with the ambient ions and electrons, both of which decrease in density with increases in the SZA [e.g., Schunk and Nagy, 2000]. Unfortunately, there are no calculations or measurements of the variation of \( T_e \) or \( T_a \) with \( \chi \) in the Martian ionosphere.

The \( T_e \) profile in the Venus ionosphere has been found to be nearly independent of solar zenith angle [e.g., Miller et al., 1980]. An inverse correlation between \( n^e \) and \( T_e \) in the Venus ionosphere has, however, been found by Knudsen et al. [1979], Dobe et al. [1993], and Mahajan et al. [1994]. Breus et al. [2004] have deduced evidence from analysis of some of the MGS profiles that \( T_e \) and \( E_{10.7} \) in the Martian ionosphere are anticorrelated. \( E_{10.7} \) is the integrated solar energy flux in the 1 to 100 nm region in the S2K models, expressed in \( F_{10.7} \) units [e.g., Tobiska, 2004]. We thus might expect that at large solar zenith angles, where the peak electron densities are smaller than those at 60°, some increase in \( T_e \) may actually be realistic. The uncertainties in the electron temperature profiles are among the largest sources of error in our models. We note here also, however, that the values of \( T_e \) in the Venus ionosphere have been found to be partly controlled by the interaction of the ionosphere with the solar wind [e.g., Brace et al., 1980], and with the presence or absence of an induced magnetospheric field [e.g., Dobe et al., 1993].

Various investigators have determined the solar activity variation of the electron peak densities, generally expressed as

\[
\log n^e_{\text{max},\chi} \propto (\log F_{10.7})^m
\]

Since we have constructed models for only two values for \( F_{10.7} \), 68 and 207, we have estimated the exponents \( m \) in equation (9) from the ratio of the \( F_1 \) peak density of the high solar activity model to that of the low solar activity model for each solar zenith angle. We find that the derived values of \( m \) are 0.38, 0.36, 0.34, 0.32, 0.30, 0.29, and 0.41 for solar zenith angles of 60, 65, 70, 75, 80, 85, and 90°, respectively. These exponents are in substantial agreement with those derived by Breus et al. [2004], for a subset of the MGS orbits in occultation season 4, for their “corrected” values of the peak densities, \( n^e_{\text{max},\chi}(H_e/\cos \chi)^{0.5} \) vs \( E_{10.7} \) of 0.37 ± 0.06. For pre-MGS data, Hantsch and Bauer [1990] derived a similar value of 0.36 for the exponent in equation (9) above. This solar activity variation of \( n^e_{\text{max},\chi} \) on Mars is similar to that reported for the peak electron densities at Venus as a function of \( F_{10.7} \) by Kliore and Mullen [1989] from an analysis of 115 radio occultation profiles from the PV ORO. They derived an equation that represents a best fit to the maximum electron densities as a function of solar activity and \( \chi \):

\[
n^e_{\text{max}}(F_{\text{oro}}, \chi) = (5.92 \pm 0.03) \times 10^5 \times (F_{\text{oro}}/150)^{0.376\pm0.011}(\cos \chi)^{0.511\pm0.012}
\]

where \( F_{\text{oro}} \) is an estimated value of \( F_{10.7} \) corrected to the position of Venus. Note that the exponent of \( \cos \chi \), 0.511, is apparently “Chapman-like.”

4.3. Topside Scale Heights

In Table 5 we present the neutral density scale heights, \( H_n \), the ion (or electron) density scale heights \( H_i \), and the plasma pressure scale heights \( H_p \) at altitudes that are 33 km above the ion peaks for all of the models. Because the peak rises as the solar zenith angle increases, the altitudes at which the scale heights are evaluated also increase. Also shown in Table 5 are values for \( H_i \) and \( H_p \) at 250 km for each model. The values of \( H_n \) and \( H_i \) were determined numerically from the model neutral and electron density profiles. The values of \( H_p \) were computed as \( k(T_e + T_i)/\n_i \), where \( n_i \) is the average mass of the ions. The values of \( H_i \) and the ratios \( H_i/H_n \) at high solar activity for the 70 and 75° models are anomalously large and are artifacts that result from slope discontinuities in the ion and electron temperature profiles, which are shown in Figure 2.

In Chapman theory, the atmosphere is assumed to be isothermal. The values of \( H_n \) at the peaks, as shown in Table 3, are, however, significantly smaller than those 33 km above the peak, as shown in Table 5. This reflects mostly the rise of the assumed neutral temperatures in this region of the model. The scale height is also inversely proportional to the acceleration of gravity, which decreases slowly with altitude, but this contributes negligibly to the increase in scale heights over a 33 km altitude range.

The ratios of \( H_i \) to \( H_n \) at 33 km above the ion peak are listed in the fifth column of Table 5. Chapman theory (equation (5)) suggests that the ion density scale heights above the peak should be twice the neutral density scale heights. The model ratios \( H_i/H_n \) for low solar activity vary from 2.3 to 1.19, as the SZA increases from 60 to 90°. The larger values for 60° SZA are also related the non-Chapman factors discussed earlier which cause the broadening of the peaks. The values of \( H_i \) and the ratios \( H_i/H_n \) ratio decrease sharply with increasing SZA for values greater than 80°. This is because the altitudes at which the scale heights are computed are above the PCE region, where the ion densities decrease at a larger rate owing to the upward flux boundary conditions at the top of the model [cf., Chen et al., 1978; Fox, 1993, 1997]. Thus the ratio \( H_i/H_n \) falls below 2 for the larger solar zenith angles. The values of \( H_i \) should also deviate from twice the neutral scale height because the ion density depends on the dissociative recombination coefficient, which is proportional to \( T_e^{0.35} \). As noted previously, the model electron temperatures at the electron density peaks increase with altitude. This is also true at altitudes above the peak. This effect has also been noted by Hantsch and Bauer [1990], Zhang et al. [1990], and Breus et al. [2004].

Table 5 also shows that the values of \( H_i \) are significantly less than those of the plasma pressure scale height.
Table 5. Model Topside Neutral, Ion and Plasma Pressure Scale Heights at 33 km Above the Peak and at 250 km, as a Function of SZA, km, and ratio of $H_p$ and $H_m$.

<table>
<thead>
<tr>
<th>SZA</th>
<th>Altitude, km</th>
<th>Neutral Scale Height</th>
<th>Ion Scale Height</th>
<th>Ratio</th>
<th>Plasma Pressure Scale Height</th>
<th>Ion Scale Height</th>
<th>Plasma Pressure Scale Height</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Low Solar Activity</td>
<td></td>
<td></td>
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<tr>
<td>$60^\circ$</td>
<td>169</td>
<td>11.4</td>
<td>25.8</td>
<td>2.3</td>
<td>44.1</td>
<td>59.7</td>
<td>287</td>
</tr>
<tr>
<td>$65^\circ$</td>
<td>170</td>
<td>11.6</td>
<td>26.3</td>
<td>2.3</td>
<td>44.9</td>
<td>59.7</td>
<td>287</td>
</tr>
<tr>
<td>$70^\circ$</td>
<td>172</td>
<td>11.7</td>
<td>26.9</td>
<td>2.3</td>
<td>45.8</td>
<td>59.7</td>
<td>287</td>
</tr>
<tr>
<td>$75^\circ$</td>
<td>174</td>
<td>12.1</td>
<td>29.2</td>
<td>2.4</td>
<td>47.4</td>
<td>59.7</td>
<td>287</td>
</tr>
<tr>
<td>$80^\circ$</td>
<td>177</td>
<td>12.4</td>
<td>23.4</td>
<td>1.88</td>
<td>47.4</td>
<td>59.8</td>
<td>287</td>
</tr>
<tr>
<td>$85^\circ$</td>
<td>182</td>
<td>13.2</td>
<td>15.0</td>
<td>1.13</td>
<td>56.0</td>
<td>59.8</td>
<td>286</td>
</tr>
<tr>
<td>$90^\circ$</td>
<td>190</td>
<td>14.7</td>
<td>17.4</td>
<td>1.19</td>
<td>82.1</td>
<td>59.8</td>
<td>286</td>
</tr>
</tbody>
</table>

|     |                      | High Solar Activity |
|     |                      |                    |                  |       |                              |                  |                              |
| $60^\circ$ | 170 | 18.1 | 51.8 | 2.9 | 57.0 | 43.0 | 275 |
| $65^\circ$ | 171 | 17.7 | 54.2 | 3.1 | 57.6 | 46.4 | 303 |
| $70^\circ$ | 175 | 16.9 | 120.2 | 7.1 | 59.3 | 46.5 | 303 |
| $75^\circ$ | 177 | 17.2 | 86.0 | 5.0 | 60.8 | 46.5 | 303 |
| $80^\circ$ | 181 | 20.1 | 54.7 | 2.7 | 67.6 | 46.6 | 303 |
| $85^\circ$ | 191 | 22.0 | 36.3 | 1.65 | 101 | 46.7 | 303 |
| $90^\circ$ | 211 | 24.3 | 33.1 | 1.36 | 165 | 47.0 | 303 |

*Here, 33 km above ion peak.
*At 250 km.
*Computed as $k(T_e + T_i)\rho_i/g$, where $T_e$ and $T_i$ are the electron and ion temperatures, $\rho_i$ is the average mass of the ions, and $g$ is the acceleration of gravity.
*These points are anomalous. They are associated with slope discontinuities of the electron and ion temperature profiles.

$H_p$, both at 33 km above the ion peak and at 250 km. In a stationary ionosphere, the ion density and plasma pressure scale heights are related by

$$\frac{1}{H_p} = \frac{1}{H_i} + \frac{1}{T_p} \frac{dT_p}{dz}$$  (11)

where $T_p = (T_e + T_i)$ is the plasma temperature. Thus at altitudes where the plasma temperatures are increasing, the values of the ion density scale heights will be substantially smaller than the plasma pressure scale heights, even in the absence of the assumed upward fluxes. Therefore the ion density profiles cannot be used to determine the values of $T_e$ and $T_i$ by fitting the observed topside scale heights to the expression $k(T_e + T_i)/\rho_i g$, as they could be if the ion densities were in diffusive equilibrium in an isothermal atmosphere.

We have evaluated the solar activity variations of the ion scale height 33 km above the electron density peaks in our model by fitting the exponent $n$ in the formula $H_i \propto F_{10.7}^n$. Values of 0.63, 0.65, 0.76, 0.79, and 0.58 are determined for solar zenith angles of 60, 65, 80, 85, and 90°, respectively. These values are somewhat larger than that reported by Bauer and Hantsch [1989], who found a best-fit value for $n$ of 0.55 for the topside electron densities obtained from radio occultation measurements on the Mariner 4, 6, 7, and 9 spacecraft, the Mars 2, 3, 4, and 6 spacecraft, and in situ data from the two Viking Landers. Our derived values are based, however, on only two points for each SZA.

5. Summary and Conclusions

We have analyzed the MGS electron density profiles for seasons 1, 2, and 4, and recorded the $F_1$ and $E$ peak electron densities, the altitudes of the peaks, the solar zenith angles, and the $F_{10.7}$ values corrected for the orbital position of Mars. For each day we have selected for analysis one profile that exhibits the median $F_1$ peak density for that day. We plot the logs of the maximum densities against the log of the SZA, and present values for the slope $k$ and predicted subsolar maximum densities, $A$ ($h_{max,0}$), in equation (8). We find that for the $F_{10.7}$ range 140–190, the derived values for $k$ are $0.465 \pm 0.010$ and $0.551 \pm 0.024$, and the predicted subsolar peak densities are $(1.82 \pm 0.03) \times 10^{10}$ and $(9.4 \pm 0.4) \times 10^{5} \text{ cm}^{-3}$ for the $F_1$ and $E$ peaks, respectively. The data from the other $F_{10.7}$ ranges are not well distributed over longitude, and therefore the derived values of $k$ and $A$ are of limited validity. As more RO profiles are included in our data sets, better statistics will lead to more secure conclusions.

We have also constructed models of the low and high solar activity Martian thermospheres/ionospheres for solar zenith angles from 60 to 90° in 5° intervals. The background neutral atmospheres are similar to those that we have adopted recently [Fox, 2004]. We have presented altitude profiles of the ion production rates from photoionization and electron impact ionization, and the resulting total ion or electron densities. As expected, the profiles exhibit two peaks, which are somewhat smaller in magnitude than those measured by the MGS radio science measurements. As explained previously, we attribute this to the use of the S2K 2.22 solar flux model of Tobiska [2004], which gives ion peak densities that are 20–30% smaller than those obtained using the S2K v1.24 solar flux model, or the Hinteregger solar fluxes that we have used previously [Fox, 2004]. We also find that the model $F_1$ peaks for solar zenith angles less than $\sim 85°$ are considerably higher in the atmosphere than the radio occultation peaks for nondusty conditions. This implies that the neutral temperatures and densities at a given angle do decrease somewhat as the terminator is approached. We have fitted the model maximum electron densities as a function of cos $\chi$ to the Chapman formula, equation (8), and predict values of the slope $k$ and the intercept $A$. Our derived values for $k$ are 0.43 and 0.46 for the high solar activity model $F_1$ and $E$ peaks, respectively and 0.36 and 0.43 for the low solar...
activity $F_1$ and $E$ peaks, respectively. All the model $k$ values are less than the “Chapman” value of 0.5. We argue, however, that the use of spherical geometry by itself causes the value of $k$ to decrease below the Chapman value, as expressed by equation (8), in the near-terminator region. Thus a perfect Chapman profile in the near terminator region would be characterized by a value of $k$ that is less than 0.5.

[77] That the model values of $k$ are smaller than those derived from the MGS electron density profiles, which are all in the near terminator region, is more important. The peak magnitudes and heights depend on the altitude profiles of $T_n$, $T_i$, and $T_e$ and the neutral density profiles. That the peak altitudes are too high could partially be explained by a small vertical offset of all the models. As evidenced also by the peak altitudes, the discrepancy between the model $k$ values and those derived from the MGS data implies also that the neutral atmosphere appears to be solar zenith angle dependent. Electron temperatures that are too large and increase too strongly at the peak altitude as the solar zenith angle increases also contribute to the smaller predicted values of $k$. The variations of the $T_e$ profiles with SZA and with solar activity are among the largest uncertainties in the model. We conclude that the actual values of $T_e$ at the ion peaks probably do not increase with increasing solar zenith angle as rapidly as they do in our models.

[78] We also argue that there are factors due to the expected non-Chapman behavior, that broaden and reshape the electron density profiles, which limits the accuracy of values of $H_n$, or $T_e$ derived by fitting the measured electron density profiles in the region of the peak to theoretical Chapman profiles. This broadening of the peak, along with the increase in $T_e$ above the peak also leads to inferred values of ion scale heights $H_i$ 33 km above the peak that are larger than twice the value of $H_n$ at the peak for the smaller solar zenith angles models. For larger solar zenith angles, the ratio $H_i/H_n$ is less than 2 because the altitude where $H_i$ is evaluated is above the PCE boundary. The ion or electron scale height in this region is decreased due to the assumption of upward flux boundary conditions, which probably reflect the interaction of the solar wind with the thermosphere. We also find that the peak densities for the 90$^\circ$ models are near or above the PCE boundary. Therefore fitting the electron density profiles for solar zenith angles approaching or larger than 90$^\circ$ to Chapman profiles may be inappropriate.

[79] Solar activity variations of the model $F_1$ peaks as expressed by the exponents $m$ in the expression $n_{\text{max},i} \propto (\log F_1)^m$ which range from 0.29 to 0.41 for the seven solar zenith angle models are in good agreement with those derived by other workers. The values of the exponent are also similar to the value of 0.376 ± 0.011 derived for Venus by Kliore and Muller [1989].

[80] Finally, we note that unlike many of the MGS profiles, our models exhibit a shoulder rather than a distinct minimum between the $F_1$ and $E$ peaks, as shown by the profiles in Figures 1 and 9. This is a subject for further study.

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