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A Genetic Optimization Approach for Isolating Translational Efficiency Bias

Douglas W. Raiford, Dan E. Krane, Travis E.W. Doom, and Michael L. Raymer

Abstract—The study of codon usage bias is an important research area that contributes to our understanding of molecular evolution, phylogenetic relationships, respiratory lifestyle, and other characteristics. Translational efficiency bias is perhaps the most well-studied codon usage bias, as it is frequently utilized to predict relative protein expression levels. We present a novel approach to isolating translational efficiency bias in microbial genomes. There are several existing methods for isolating translational efficiency bias. Previous approaches are susceptible to the confounding influences of other potentially dominant biases. Additionally, existing approaches to identifying translational efficiency bias generally require both genomic sequence information and prior knowledge of a set of highly expressed genes. This novel approach provides more accurate results from sequence information alone by resisting the confounding effects of other biases. We validate this increase in accuracy in isolating translational efficiency bias on 10 microbial genomes, five of which have proven particularly difficult for existing approaches due to the presence of strong confounding biases.

Index Terms—Codon usage bias, evolutionary computing and genetic algorithms, miscellaneous, artificial intelligence, computing methodologies, GC-content, strand bias, translational efficiency.

1 INTRODUCTION

Conventional wisdom has held that natural selection differentiates among alleles based upon the competitive advantage or disadvantage conferred by mutations that result in changes to the end product of the gene [1]. Recent work, however, has revealed that selective advantage can be present at a much finer level than was previously appreciated. An example of a subtle, genomewide trend that can confer such a selective advantage is the biased usage of codons [2], [3], [4]. Because the genetic code is degenerate (with many amino acids coded for by multiple synonymous codons), there exists the possibility for species to use some codons preferentially, while eschewing others. Microbial organisms can exhibit bias toward increased (or decreased) usage of G and C nucleotides (content bias), bias induced by differential mutation rates along the leading and lagging strands during DNA replication (strand bias), and bias toward codons associated with more common tRNAs (translational efficiency bias). The latter—a tendency to use codons associated with common tRNAs—is assumed to confer more efficient translation of highly expressed genes. The resulting bias has been shown to have a subtle, genomewide effect upon many simple organisms.

The study of translational efficiency codon usage bias has proven to be an important research topic. The degree to which a gene adheres to translational efficiency bias has been shown to correlate with the gene’s expression level in many Bacteria [4], [5], [6] and some low-order Eukarya [7], [8]. This trait has been exploited in studies that have used adherence to translational efficiency bias as a proxy for expressivity [9], [10], [11], [12]. Use of translational efficiency bias as a surrogate for expressivity is useful, in part, because experimental methods for obtaining transcript or protein abundance (such as that provided by oligonucleotide microarrays or gel electrophoresis) are relatively expensive in terms of time, materials, and reagent cost. Estimating expressivity using translational efficiency bias may provide an additional benefit in that experimental methods provide measures of transcript or protein abundance, not the underlying production rates. Additionally, knowledge of codon adaptiveness associated with translational efficiency can be employed to maximize the yield of heterologous protein production (genes introduced into a host organism’s genome for the purpose of producing recombinant protein) [13], [14]. By modifying the introduced gene to conform to the host organism’s codon usage bias, an increase in protein product can be realized [15].

One of the earliest methods for determining adherence to translational efficiency bias did so first by examining highly expressed genes to identify which codons were preferred, and then calculating the frequency of optimal codon usage (FOP) for the genes in the genome [5]. It was shown that FOP was highly correlated with protein expression levels in some Bacteria. This is a binary interpretation of codon preference. Either the codon is identified as optimal, or it is not. Later, the measurement of adherence to translational efficiency bias was refined by introducing gradation to the process. The concept of degree of preference, or the degree to which a codon has adapted, was introduced with the codon adaptation index (CAI) measurement [16].
genes to determine codon preference) are susceptible to the ods that use the codon counts in a set of highly expressed translational efficiency bias identification methods (meth-
ods that use the codon counts in a set of highly expressed translational efficiency bias identification methods (meth-
s). These tally-based methods rely upon the uniform conformance of highly expressed genes to the underlying translational efficiency bias in order to identify the degree of preference for each codon. However, the adherence of highly expressed genes to translational efficiency bias is far from uniform. As an example, on average, only 58 percent of the highly expressed genes for *Saccharomyces cerevisiae* prefer the codon that is preferred "overall." This lack of uniformity can result in a reduced ability to predict expressivity. Fig. 1 shows the predicted placement of the most highly expressed genes in a sorted list of all the genes in two genomes (one known to have translational efficiency bias as the dominant bias and one thought to exhibit little or no translational efficiency bias but strong GC-content and strand biases). The degree to which the highly expressed genes fall in the lower regions of the sorted lists is an indication of prediction error. This error is particularly pronounced in organisms with genomes that exhibit codon usage trends dominated by a bias other than that of translational efficiency bias (Fig. 1b). Throughout the rest of this paper we refer to these organisms as confounded. In Section 3, specific criteria are presented for determining whether an organism is confounded or not. All tally-based translational efficiency bias identification methods (meth-
ods that use the codon counts in a set of highly expressed genes to determine codon preference) are susceptible to the confounding effects of other biases (such as content or strand bias) simultaneously influencing codon selection. The direct search-based approach described here resists these confounding effects. Through the use of this methodology, translational efficiency bias can be identified in genomes previously thought not to exhibit this bias. Also, improvements in expression prediction can be realized for organisms where other biases confound the isolation process. The effectiveness of the approach is tested on 10 genomes. Five of these genomes are known to be dominant for either GC- or AT-content (and in two cases, also dominant for strand bias) and are believed to exhibit weak or nonexistent translational efficiency bias. The remaining genomes are dominant for translational efficiency bias [17]. The performance of the approach is assessed by comparing the resultant CAI score gene rankings with that of experimentally determined expression data.

2 Methods

The direct search-based approach operates similarly to the traditional CAI technique [16]. The traditional method uses a tally-based approach to determine the degree of preference, or weight, for each codon by examining a set of highly expressed genes. A codon with a high degree of usage in the highly expressed genes is assigned a relatively large weight. The direct search approach, instead, searches for weights that explain the high adherence scores of the highly expressed genes. In both approaches, these weights are then used to measure the adherence of the rest of the genes in the genome.

2.1 Reference Sets

Both the traditional CAI calculation method and the direct search-based approach described here rely upon the identification of a set of genes (the reference set) that is determined experimentally (or known, generally) to compr-
ise the most highly expressed genes of the genome. The direct search-based approach uses as a reference set the most highly expressed genes as determined from experimental microarray expression data (Section 2.8) or as determined through the use of a high-expression database (HEDB, Section 2.4). In the case of the experimentally determined highly expressed (EDHE) genes, the size of the reference set is set to 1 percent of the genes in the genome. This size was chosen because it roughly corresponds to the size of reference sets proposed by the authors of [6], [7], [16], [18], [19], [20]. In the case of the HEDB-determined reference set, the size is set by the number of hits returned from the database. These reference sets and reference set sizes are the same for both the traditional CAI and the genetic algorithm methods when they are compared.

2.2 CAI

The Sharp and Li [16] CAI approach assigns a value known as the relative adaptiveness (or weight) to each codon. The weight for each codon is derived from the codon usage frequencies of genes in the reference set. These frequencies are normalized by the average usage for the set of synonymous codons related to the codon in question. This normalized frequency is known as relative synonymous
codon usage (RSCU) [21], (1). The RSCU and the weight of a codon $w_{ij}$ are:

$$RSCU_{ij} = \frac{X_{ij}}{\sum_{j=1}^{n_i} X_{ij}},$$

(1)

Normalized $RSCU = w_{ij} = \frac{RSCU_{ij}}{RSCU_{i\text{max}}} = \frac{X_{ij}}{X_{i\text{max}}}$. (2)

$X_{ij}$ is the count of the codon within the subset of genes known as the reference set, and $X_{i\text{max}}$ is the count of its sibling (siblings are codons from the family of codons that code for a given amino acid) with the highest count (the maximal sibling will have a weight of one). $w_{ij}$ is the weight $w$ of the $i$th codon for the $j$th amino acid. To determine the CAI of a particular gene, the geometric mean of the normalized RSCU value (or weight) for each codon in the gene is calculated (3). Here, $L$ is the length of the gene (in codons)

$$CAI(g) = \prod_{i=1}^{L} w_i.$$

(3)

2.3 Ribosomal Criterion

To determine whether an identified bias is, specifically, a high-expression bias, it is necessary to show that rarely expressed genes adhere strongly to that bias. Carbone et al. [17] have developed a measure that can help determine whether an identified bias is representative of translational efficiency. The measure is known as the ribosomal criterion. This criterion is based on the degree to which the ribosomal protein coding genes (which may be assumed to be highly expressed) are found in the upper region of a list of genes sorted by CAI value. Carbone et al. conclude that the identified bias is that of translational efficiency when the average CAI value for the organism’s ribosomal protein coding genes (RPCGs) is greater than one standard deviation above the mean CAI value for the organism’s genome

$$z = \frac{(CAI(r) - \bar{CAI})}{\sigma_{CAI}},$$

(4)

where $CAI(r)$ is the CAI score of a given ribosomal protein coding gene. The average of the $z$-scores for all RPCGs (4), $\bar{z}$, is the ribosomal criterion. A genome characterized by translational efficiency bias would be expected to have a high $\bar{z}$.

2.4 High-Expression Database

Recently, sequenced genomes may not have identified ribosomal protein coding genes. To allow for this contingency, we have developed a database of highly expressed proteins (HEDB) that can be used to identify homologs within the target genome [22]. The proteins chosen for the database are ribosomal proteins, elongation factors, and RNA polymerase subunits (excluding the sigma subunit). These were chosen because they are known generally to be highly expressed, and they tend to exhibit high overall average CAI scores in well-characterized genomes (extensively studied genomes whose dominant bias is known to be translational efficiency, data not shown).

An unfiltered blast search is performed [23] to identify probable highly expressed genes in a target genome. This search is performed for each gene in the target genome, using the corresponding protein as a query against the HEDB. The query protein is considered to be a homolog of database proteins with 60 percent identity. The database currently contains proteins from 66 organisms. The organisms used to build the HEDB are drawn from 25 different bacterial taxonomical subclasses, or groups, in order to achieve a classwide representative sampling. The database contains no proteins from organisms used as target genomes in this study to guarantee independence between the genomes being analyzed and the HEDB.

2.5 Strength Criterion

A characteristic of a genome with a strong, dominant bias of translational efficiency is that the most highly expressed genes (the reference set) tend to be much more highly biased than the rest of the genome. The presence of this condition (of a strongly biased reference set) can be further evidence that a detected bias is that of translational efficiency bias. The CAI weights associated with the reference set are an indication of the strength of this bias. As an example, consider the strongest possible bias that could be exhibited. The maximal sibling will always have a weight assignment of one. The strongest possible bias would yield weights of zero for the rest of the siblings. Weaker biases would have nonmaximal sibling weights closer to one. Thus, one measure of the strength of the bias is indicated by how far the weight vector (vector comprised of the 64 codon-associated weights) deviates from balanced usage. Another, perhaps more useful, measure is how much more biased the weight vector is from the overall bias of the organism. Carbone et al. [17] developed such a criterion for measuring bias strength (5)

$$d(w^G, w^S) = \sum_{i=1}^{64} \frac{|w_i(G) - w_i(S)|}{2}.$$  (5)

The overall bias of the organism is obtained by extracting the weight vector generated using the entire genome as the reference set ($w^G$). This is compared to the weight vector of the smaller reference set containing only highly expressed genes ($w^S$). The result can be thought of as measuring the number of codon families where the preferred codon is different in two biases.

Consider a case of a binary weight vector (each family has a single weight of one and the rest zero) where the major codons change for all families between $G$ and $S$. This yields a summation of the differences (Manhattan distance) of 40. Dividing by two brings the number back to the number of changed major codons (20). In other words, (5) is equal to one-half the Manhattan distance.

A genome characterized by translational efficiency bias should have a relatively large strength measure. Carbone et al. [17] set the criterion for an organism’s bias to be considered strong at $d(w^G, w^S) > 8$, but they note that not all organisms characterized by translational efficiency bias meet this criterion. Instead, they use it in conjunction with the ribosomal criterion to differentiate weak and strong translational efficiency bias.

2.6 Direct Search-Based Approach

The direct search-based approach differs from the traditional method in the way in which the weights are determined.
Instead of assigning weights based upon the codon usage of the reference set, a genetic algorithm performs a computational search for an optimal set of weights. The search looks for a set of weights that optimizes the placement of the reference set in a sorted listing of genes according to their adherence to the bias defined by the weights.

A genetic algorithm is an optimization technique modeled after nature’s approach to maximizing a species’ fitness for survival and reproduction [24], [25]. The algorithm simulates natural selection by maintaining a population of individual members, each of which is a proposed solution to the given search problem. The search for the best solution proceeds by selecting members from the population to produce offspring that combine traits from the parents. A fitness score is assigned to each proposed solution and poor solutions are removed from the population in a process that mimics natural selection. Offspring in nature vary from their parents through recombination of the parents’ DNA (also known as crossover) and through the occurrence of genetic mutations. In order to imitate this behavior, the GA must have a representation of the solution that is amenable to these operations (crossover and mutation).

### 2.6.1 Representation

The search being performed is for a set of weights. These weights are represented as a 64-dimensional (one for each codon) vector that contains real-valued weights. The GA will search for weights that produce high CAI scores in high-expression genes and lower scores for the rest of the genes in the genome.

### 2.6.2 Selection of Parents

Identification of the parents for the purposes of recombination is performed using tournament selection [26]. Candidates are chosen at random until a tournament size of three is achieved (tournament size of three was chosen with the intent to impose a small degree of selective pressure so as to avoid premature convergence to local optima). The member with the best fitness within this group of three is the tournament winner and is selected as a parent. Once two parents are identified, crossover (Section 2.6.3) is employed to generate a child chromosome. This is followed by a mutation operation (Section 2.6.4) to add additional variation into the population.

### 2.6.3 Crossover Operator

Crossover between two population members with more simple representations (such as bit strings) can be achieved by choosing the contents from one of the parents at each gene (bit) location, and inserting it into the appropriate position of the offspring’s bit string. While this is a viable approach in real-valued vectors, there are other, often more effective, techniques in real vector spaces [27]. Simply populating the offspring with entries from each parent can cause wild, unpredictable jumps in the search space. Instead, if a point is chosen that is somewhere between the two chromosomal vectors, such as a midpoint or a weighted midpoint, then crossover can become a more meaningful search operation in many real-valued vector spaces.

The GA described here employs geometric crossover as described in [28] where the entry in the offspring’s real-valued vector is the geometric mean of the two parents. This method was chosen because the geometric mean favors the smaller weight (the conservative choice in terms of choosing most preferred codons). This is due to the “fundamental inequality” (the geometric mean is never greater than the arithmetic mean). Additionally, this is similar to the way in which CAI is determined; it is the geometric mean of the weights associated with the codons in each gene.

### 2.6.4 Mutation Operator

Mutation is achieved by slightly perturbing each weight within the weight vector. The new weight is a randomly generated real number normally distributed about the current weight. Equation (7) demonstrates the generation of a mutated weight $w'_i$ from the original weight $w_i$. $N$ is a function that generates a random number that is normally distributed about a mean ($\mu$) with a given standard deviation ($\sigma$). $i$ is the index that identifies which of the 64 dimensions in the vector is associated with the weight in question. The mutation is self-limiting to a value that is no greater than one. For the GA described here, the standard deviation of the random normal probability distribution function is greater in the early generations and less during the late generations. This is related to the process of simulated annealing [29], [30]. This slow decrease in $\sigma$ allows for greater “jumps” early in the search process and smaller steps during the latter stages. For the purposes of this GA, the standard deviation ($\sigma$) for a given generation ($\text{gen}_{\text{current}}$) is determined as in (8), where $\text{gen}_{\text{final}}$ is the number of generations that the GA will be allowed to run, $\sigma_0$ is the starting standard deviation (the standard deviation at generation zero), and $b$ is a parameter that changes the shape of the curve described by the function. The GA described here uses a $b$ parameter of one and an initial standard deviation of 0.3. The $b$ value of one is chosen to generate a simple linear decrease in the degree of mutation with respect to generation number. A beginning standard deviation of 0.3 is chosen to distribute the initial mutation-introduced variance normally with room for mutations of up to three standard deviations. The weight scale is from zero to one; this allows three standard deviations of size 0.3 to fit within this range:

$$w'_i = \begin{cases} 1, & \text{if } w'_i > 1, \\ \varepsilon, & \text{if } w'_i \leq 0, \\ w'_i, & \text{otherwise}, \end{cases}$$

$$\sigma = \sigma_0 \times \left(1 - \frac{\text{gen}_{\text{current}}}{\text{gen}_{\text{final}}}\right)^b.$$
greater than zero (7). An ε value (in (7)) of 0.0001 was chosen to allow for relatively small weight values. While the crossover and mutation operators will never generate weights greater than one, they may cause a maximal sibling to have a value less than one. Therefore, a repair operator was developed that sets the maximum weight in each codon family to one, and it increases the weight for each family member an amount proportional to the increase of the maximal sibling. Equation (9) represents the repair performed to weight \( w_i \) at each dimension \( i \). The original weight for the maximal sibling is \( w_{\max, \text{sib}} \). The maximal sibling weight is normalized to one. All other weights will be increased (or will remain the same) when divided by this value (as all weights are less than or equal to one)

\[
w'_i = \frac{w_i}{w_{\max, \text{sib}}}.
\]

### 2.6.6 Fitness Function

The goal of the GA is the discovery of a set of weights that produces a ranked listing of genes (by CAI score) that matches the expectation that highly expressed genes will be highly ranked in such a listing. The technique devised to measure this property is rank fitness. The genes are sorted by CAI score and an index is assigned to all genes. The gene with the smallest CAI value is assigned an index of 0 while the gene with greatest CAI value is assigned an index of \( N - 1 \), where \( N \) is the number of genes in the genome. The indexes of the reference set genes are summed (IDXs in (10)) and this number is normalized by the maximum attainable rank fitness value (11) yielding a value between 0 and 1 representing the degree to which the reference set rises to the top of a sorted (by CAI score) list of genes (12)

\[
f(RS) = \sum_{i=1}^{[RS]} \text{IDX}_i,
\]

\[
f_{\text{max}}([RS]) = \sum_{i=N-[RS]}^{N-1} i,
\]

\[
f_{\text{norm}}(RS) = \frac{f(RS)}{f_{\text{max}}([RS])}.
\]

### 2.6.7 Initializing the Population

The population weights begin with values that are defined using the traditional method (CAI, Section 2.2) and then mutated following a normal distribution with a 0.01 standard deviation. This value is chosen to introduce a fairly small amount of variance into the initial population. This results in the search process beginning in the neighborhood of the weights as determined by the Sharp & Li method [16].

The GA population size is set at 100 with the number of offsprings also set at 100. Population management follows that described by Bäck et al. [31] as \((\mu + \lambda)\) where \(\lambda\) offsprings are generated from \(\mu\) parents and combined into a single population in which both parents and children must compete for survival. A degree of elitism is introduced as in [32] by maintaining a certain number of the best members of the combined population in the next generation. We set this elitism parameter to 10 percent. The remaining 90 slots in the next generation’s population are selected using a fitness proportional (roulette) selection technique [33], where the more fit the individuals in the combined population are, the more likely they are to be drawn into the following generation. The elitism setting of 10 percent was chosen arbitrarily with the intent of maintaining at least a sampling of the very best solutions from one generation to the next.

### 2.7 Selection of Target Genomes

The organisms in this study were chosen to demonstrate that the direct search-based methodology can isolate translational efficiency bias (if it exists) in organisms whose genomes are dominant for either translational efficiency bias or some other, confounding bias. The organisms were drawn from those listed in a previous study that identified their dominant biases [17]. Additionally, the genomes chosen have experimental expression data available (Section 2.8). The search-based approach is validated on 10 organisms. Nine of the 10 organisms are Bacteria while one (Halobacterium sp. NRC-1) is an Archaean. Five of the genomes used for validation are known to be dominant for biases other than translational efficiency (Table 1) and, heretofore, were thought to exhibit weak or nonexistent translational efficiency bias. The remaining five genomes in this study are thought to be dominant for translational efficiency bias.

### 2.8 Microarray Data

The overall objective of the search-based approach is to identify a weight vector that captures a bias in codon usage associated with translational efficiency. Such a bias can be expected to correlate well with the expressivity of the genes in the organism’s genome. An independent estimator of the expressivity of the genes is needed to measure the effectiveness of the direct search-based approach in finding a high-quality set of weights. This allows comparison with other methods in terms of ability to identify a bias that correlates well with gene expressivity. Snapshots of mRNA expression levels, such as those obtained using microarray techniques, are one such estimator for the expressivity of each gene.

Expression data are retrieved from the NCBI Gene Expression Omnibus [34] (accession numbers GSE5400, GSE4896, GDS1469, GSE2983, GSE2667, GSE7070, GDS1099, GSE2823, and GSE3876). For Nostoc, expression data are instead retrieved from Wünschiers’ Hydrogen Database (HyDaBa) which focuses on gene expression data from the filamentous nitrogen-fixing cyanobacterium Nostoc PCC 7,120 [35]. In dual-channel experiments, the results from
the reference channel are utilized (no treatment or pre). For *Escherichia coli* K12, those trials using glucose as the carbon supply are used. When raw data are provided, background is subtracted from signal and user-determined flags and thresholds are accepted. For preprocessed data, genes listed as absent are removed from consideration.

2.9 Sequence Data

The sequence information required for calculating weights and the corresponding CAI values are derived from annotated whole genome files located in the complete microbial genomes database on the NCBI Web site (http://www.ncbi.nlm.nih.gov/genomes/lproks.cgi).

2.10 Implementation and Hardware

Genetic algorithms lend themselves to a high degree of parallelism [36]. A simple technique is to manage the population on a central computing node (parent selection, crossover, mutation, etc.) and to compute fitness concurrently on satellite nodes. This is the strategy employed in our implementation. The GA manager and fitness calculator components described here are written in C++. The jobs are presented to the remote hosts in the form of real-valued weight vectors sent over a socket connection while the results are returned over the same socket connections in the form of “long float” data types (64-bit IEEE floating-point standard format).

3 Results

In order to demonstrate that the search-based approach operates effectively in situations where experimental expression data is present and where it is not, two sets of results were generated; one where the placement of experimentally determined highly expressed genes (*CAI*<sub>opt</sub> EDHE) were maximized, and one that maximized the placement of genes identified using the HEDB (*CAI*<sub>opt</sub> HEDB).

For each of these approaches (*CAI*<sub>opt</sub> EDHE and *CAI*<sub>opt</sub> HEDB), two sets of results were generated; one for organisms dominant for translational efficiency bias (ribosomal criterion > 1 when isolated using traditional methods), and another for organisms dominant for either GC- or AT-content, and/or strand bias (as determined by the reference channel).

The performance of the direct search-based approach on the genome for *C. jejuni* is particularly noteworthy. For the other organisms, the traditional method of calculating CAI, while confounded (ribosomal criterion ≤ 1 and dominant for content and/or strand bias), nevertheless exhibits a significantly positive correlation with experimentally determined expression data. *C. jejuni* exhibits no such significant trend when traditional CAI is employed. The search-based method, however, is able to disambiguate the translational efficiency bias from the high AT-content and strand biases and yields a ribosomal criterion > 1 and a significantly
positive Spearman rank correlation with transcript abundance data (Table 3).

3.2 Search Process

A fitness history (Fig. 2) shows that dramatic improvements in rank fitness occur very quickly in the search process. As the GA converges on the final solution, the other population members begin approaching similar rank fitness values to the best in the population (average, median, and worst population members begin approaching the best population member’s fitness).

3.3 Comparison of Summary Data

As the GA works by maximizing rank fitness for a given reference set, it stands to reason that the rank fitness values will be greater for the search-based approach than for the traditional method of determining CAI. Less obvious is the effect that this search strategy would have on ribosomal criterion and bias strength. Figs. 3 and 4 demonstrate that the direct search-based approach identifies a bias that is both stronger and that exhibits higher ribosomal criterion than the biases identified by traditional methods. Comparisons are made between techniques that use the same reference set genes, though other combinations yield similar results (data not shown).

To summarize the effectiveness of the direct search-based approach in the dimensions of strength criterion, ribosomal criterion, rank fitness, and Spearman rank correlation coefficient, we perform principal components analysis [39], [40], and then project the original data onto the first two principal components (Figs. 5 and 6). There is clear separation between the search-based and CAI data for confounded organisms providing visual support for the improved performance of the direct search-based method in all of these dimensions.

A series of t-tests are employed to determine whether the search-based criteria are statistically greater than those of traditional CAI (Table 6). All $p$-values are less than 0.05 except those associated with tests between $r_S$ values for unconfounded organisms. The $p$-values for the $r_S$ values are

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### Table 3

**Performance Measurements for Genetic Algorithms (Confounded Organisms)**

<table>
<thead>
<tr>
<th>Organism</th>
<th>$r_S$</th>
<th>$RF$</th>
<th>$r_S$</th>
<th>$RF$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Campylobacter jejuni NCTC 11168</td>
<td>0.093</td>
<td>0.17</td>
<td>0.970</td>
<td>0.003</td>
</tr>
<tr>
<td>Halobacterium sp. NRC-1</td>
<td>0.388</td>
<td>0.17</td>
<td>0.861</td>
<td>0.007</td>
</tr>
<tr>
<td>Nostoc sp. PCC 7120</td>
<td>0.324</td>
<td>0.03</td>
<td>0.968</td>
<td>0.003</td>
</tr>
<tr>
<td>Pseudomonas aeruginosa PAO1</td>
<td>0.444</td>
<td>0.007</td>
<td>0.968</td>
<td>0.002</td>
</tr>
<tr>
<td>Streptomyces coelicolor A3(2)</td>
<td>0.149</td>
<td>0.006</td>
<td>0.743</td>
<td>0.003</td>
</tr>
</tbody>
</table>

CAI$_{opt}$: Results for determining CAI values using the GA that optimizes weights by maximizing the placement of experimentally determined highly expressed genes. CAI$_{opt}$ HEDB: GA results that maximize the placement of HEDB genes. $r_S$: Average Spearman rank correlation coefficient over 10 runs. $RF$: Average rank fitness values over 10 runs. $r_S$ standard deviation for Spearman rank correlation coefficients. $RF$ standard deviation for rank fitness values. All Spearman rank correlation coefficients are significant ($p < 0.05$). $r_S$ value significantly more positive than that of CAI HEDB. $r_S$ value significantly more positive than that of CAI EDHE. (traditional approach, Table 5). Significance between $r_S$ values determined using a two-tailed Fisher z-transform [37] with 1.06 in the numerator of the variance calculation due to $r_S$ being nonparametric [38].

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### Table 4

**Performance Measurements for Traditional CAI (Unconfounded Organisms)**

<table>
<thead>
<tr>
<th>Organism</th>
<th>$r_S$</th>
<th>$RF$</th>
<th>$r_S$</th>
<th>$RF$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bacillus subtilis subsp. subtilis str. 168</td>
<td>0.159</td>
<td>0.730</td>
<td>0.121</td>
<td>0.958</td>
</tr>
<tr>
<td>Chlamydomphila pneumoniae AR39</td>
<td>0.230</td>
<td>0.754</td>
<td>0.228</td>
<td>0.877</td>
</tr>
<tr>
<td>Escherichia coli K12</td>
<td>0.501</td>
<td>0.903</td>
<td>0.496</td>
<td>0.910</td>
</tr>
<tr>
<td>Lactococcus lactis IL403</td>
<td>0.403</td>
<td>0.935</td>
<td>0.417</td>
<td>0.930</td>
</tr>
<tr>
<td>Shewanella oneidensis MR-1</td>
<td>0.286</td>
<td>0.919</td>
<td>0.323</td>
<td>0.942</td>
</tr>
</tbody>
</table>

CAI EDHE: CAI determined using the traditional Sharp and Li approach using experimentally determined highly expressed genes as a reference set. CAI HEDB: CAI determined using the traditional Sharp and Li approach using HEDB genes as a reference set. $r_S$: Spearman rank correlation coefficient with experimentally determined expression data. $RF$: Rank fitness value (10). All Spearman rank correlation coefficients are significant ($p < 0.05$). $r_S$ value significantly more positive than that of CAI$_{opt}$ EDHE (Table 2). $r_S$ value significantly more positive than that of CAI$_{opt}$ HEDB. Significance between $r_S$ values determined using a two-tailed Fisher z-transform [37] with 1.06 in the numerator of the variance calculation due to $r_S$ being nonparametric [38].
of particular interest. These tests indicate whether we should have statistical confidence that the direct search-based approach provides a better predictor of expressivity than the traditional tally based methods. The search-based approach performs significantly better than traditional methods of determining CAI (Table 6) on confounded organisms. $p$-values of two-tailed, paired t-tests between search-based $r_S$ values and traditional CAI $r_S$ values are significant ($\alpha = 0.05$) for confounded organisms for both EDHE and HEDB gene reference sets. This is strong
evidence that the direct search-based method is the preferred approach on confounded organisms.

3.4 Cross Validation

The direct-search methodology described here does not build a model that is then used on future genomes. Solutions for isolating translational efficiency identified by this approach are unique to each organism’s genome. As such, the concept of a training and test set for use in cross validation is not applicable to this problem domain. However, the underlying purpose of cross validation is to reinforce confidence in the approach by showing evidence of consistent performance in multiple trials, and to show the absence of overfitting.

We achieve these same goals by validating our results against experimentally determined expression data (Tables 2 and 3) and then comparing the predictive ability of the search-based approach to traditional methods (Tables 4 and 5). Due to the stochastic nature of the search process, we validate consistency by executing multiple (10) trials per organism and then showing uniformity in the results across the runs (low standard deviations in Tables 2 and 3, and low standard deviations in Figs. 3 and 4). We do this for 10 different organisms (five of which are confounded by at least one competing bias, two by multiple biases, Table 1) and use two different approaches for identifying highly expressed genes (high-expression database and experimentally determined highly expressed genes). In addition to measuring the predictive capability of the search-based approach, we examine other attributes of the solutions to determine if they are consistent with that of translational efficiency bias (i.e., strength of bias and high bias adherence scores in ribosomal protein coding genes, Figs. 3 and 4).

To validate the similarity of solutions across multiple runs, analysis was performed on the resultant weight vectors. The variance in the weights across the 10 runs was calculated, and the outcomes averaged for the 10 different genomes, the two different maximized reference sets (HEDB and EDHE), and across all codons. The average variance in the weights was a remarkably low 0.021 (the range is from 0 to 1 for the weights). This is an indication that the solutions across runs are very similar. In almost all cases, the codons identified as major (those with a weight of one) are the same across all 10 runs (variance of zero).

It is worth mentioning that trials were successfully run where randomly chosen subsets of genes (representing 90 percent of each genome) were used to identify optimal weights (fitness was correlated with actual expression values) (data not shown). These trials allowed for 10-fold cross validation; however, this approach is not applicable to the problem of predicting expression utilizing sequence information alone since expression data were required for the training set. The genetic algorithm described here requires no (and has no access to) prior knowledge of expression levels.

4 DISCUSSION

The direct search-based algorithm presented here directly seeks a set of codon preferences (weights) that yield high adherence scores in the genes known (EDHE) and presumed (HEDB) to be highly expressed (relative to the rest of the genes in the target genome). In this way, we identify a set of weights that may be more representative of the underlying tRNA abundance values, and therefore, the relative selective pressure associated with choosing each codon. These weights lead to more accurate predictions of expressivity. This approach is tested on two sets of microbial genomes, one known to be dominant for some confounding bias or biases (Table 1), and one dominant for translational efficiency bias.

Given the results of traditional CAI on the confounded organisms, one would conclude that these organisms exhibit, at best, weak translational efficiency bias (low ribosomal and strength criteria; Figs. 3 and 4). In the case of C. jejuni, one might even conclude that there is no translational efficiency bias at all (particularly in light of the negative, though nonsignificant, correlation with respect to expression levels; Table 5). For these organisms, however, the genetic algorithm finds that there is actually a strong translational efficiency bias present (ribosomal criteria > 1 and strength criteria > 8; Figs. 3 and 4). A possible cause is that the translational efficiency bias is obscured from detection when using traditional methods by other biases and by nonuniform adherence in the most highly expressed genes. The utility of these findings is supported by the expression level predictive capability of the direct search-based approach. All five of the confounded organisms are easily cultivated and exhibit exponential growth phases making the existence of translational efficiency bias unsurprising.

The search-based method performs significantly better than traditional methods of determining CAI (Table 6) on confounded organisms. p-values of two-tailed, paired t-tests between GA rS values and traditional CAI rS values are significant (α = 0.05) for confounded organisms for both EDHE and HEDB gene reference sets. For unconfounded organisms, the search-based approach performs similarly to the traditional CAI method (p-values of two-tailed, paired t-tests between GA rS values and traditional CAI rS values are 0.924 and 0.981 for EDHE and HEDB reference sets, respectively).

In addition to good performance in predicting expressivity, the direct search-based approach provides solutions that exhibit traits generally known to be shared by genomes dominant for translational efficiency bias [17]. These traits

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**Table 5.** Performance Measurements for Traditional CAI (Confounded Organisms)

<table>
<thead>
<tr>
<th>Organism</th>
<th>CAI EDHE</th>
<th>CAI HEDB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Campylobacter jejuni NCTC11168</td>
<td>rS: -0.023 RF: 0.589</td>
<td>rS: -0.004 RF: 0.745</td>
</tr>
<tr>
<td>Halobacterium sp. NRC-1</td>
<td>0.165</td>
<td>0.086</td>
</tr>
<tr>
<td>Nostoc sp. PCC 7120</td>
<td>0.046</td>
<td>0.150</td>
</tr>
<tr>
<td>Pseudomonas aeruginosa PAO1</td>
<td>0.347</td>
<td>0.303</td>
</tr>
<tr>
<td>Streptomyces coelicolor A3(2)</td>
<td>0.132</td>
<td>0.148</td>
</tr>
</tbody>
</table>

CAI EDHE: CAI determined using the traditional Sharp and Li approach using experimentally determined highly expressed genes as a reference set. CAI HEDB: CAI determined using the traditional Sharp and Li approach using HEDB genes as a reference set. rS: Spearman rank correlation coefficient with experimentally determined correlation coefficients are significant (p < 0.05) with the exception of those for C. jejuni.
include the strength of bias exhibited by the reference set, and the degree to which ribosomal protein coding genes adhere to the translational efficiency bias. Both tend to be high in organisms dominant for translational efficiency bias and are measured by strength and ribosomal criteria, respectively [ribosomal criterion > 1 (4) and strength > 8 (5)]. The strength and ribosomal criteria values for the biases identified by the search-based approach are significantly greater than those of the traditional methods for all organisms, confounded and unconfounded (p-values of two-tailed, paired t-tests between GA strength and ribosomal criterion values and traditional CAI strength and ribosomal criterion values are all less than 0.05, Table 6).

All of these factors taken together [better predictive capabilities (more positive $r_S$ values), stronger identified bias, and a gene ranking with higher ribosomal criteria] lend support for the conclusion that the direct search-based approach provides a bias identification methodology that is more indicative of the underlying translational efficiency bias than previous methods. This is true for confounded organisms, with performance equivalent to traditional methods for unconfounded organisms, whether experimentally determined high-expression genes are used as a reference set, or genes identified through the use of the high-expression database are employed. The use of the search-based method may be especially advantageous in organisms such as C. jejuni that exhibit little or no translational efficiency bias using traditional methods. Use of the direct search-based approach reveals the existence of a strong translational efficiency bias in the genome of C. jejuni (ribosomal criterion $\mu = 2.972$, $\sigma = 0.206$ and $\mu = 2.668$, $\sigma = 0.333$ for EDHE and HEDB reference sets, respectively, Figs. 3 and 4) with a significantly positive Spearman rank correlation between the GA results and experimentally determined expression data (Table 3).

All coding sequences, GA-derived weights, and GA-derived CAI values for all coding sequences (for all organisms for all runs) can be viewed or downloaded at this paper’s supplementary data Web site (http://web-dev.cs.umt.edu/cub_db/supplemental.shtml), and which can also be found on the Computer Society Digital Library at http://doi.ieeecomputersociety.org/10.1109/TCBB.2009.24.

ACKNOWLEDGMENTS

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TABLE 6

<table>
<thead>
<tr>
<th></th>
<th>EDHE</th>
<th>HEDB</th>
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<tbody>
<tr>
<td></td>
<td>$r_S$</td>
<td>S</td>
</tr>
<tr>
<td>Un-Confounded</td>
<td>0.924</td>
<td>0.004</td>
</tr>
<tr>
<td>Confounded</td>
<td>0.035</td>
<td>0.000</td>
</tr>
</tbody>
</table>

EDHE: Experimentally determined expression data used to identify reference set. HEDB: High-expression database used to identify reference set. $r_S$: Spearman rank correlation coefficient between CAI data and expression data. S: Strength criterion (5). RC: Ribosomal criterion (4).


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